

$$\text{In[1]:= } \mathbf{td} = 1 + \frac{c_1 t}{2} + \frac{1}{12} (c_1^2 + c_2) t^2 + \frac{1}{24} c_1 c_2 t^3 - \frac{1}{720} (c_1^4 - 4 c_1^2 c_2 - 3 c_2^2 - c_1 c_3 + c_4) t^4 + \frac{(-c_1^3 c_2 + 3 c_1 c_2^2 + c_1^2 c_3 - c_1 c_4) t^5}{1440} + \frac{(c_1^6 - 6 c_1^4 c_2 + \frac{11 c_1^2 c_2^2}{2} + 5 c_2^3 + \frac{5 c_1^3 c_3}{2} + \frac{11 c_1 c_2 c_3}{2} - \frac{c_3^2}{2} - \frac{5 c_1^2 c_4}{2} - \frac{9 c_2 c_4}{2} - c_1 c_5 + c_6) t^6}{30240}$$

$$\text{Out[1]= } 1 + \frac{c_1 t}{2} + \frac{1}{12} (c_1^2 + c_2) t^2 + \frac{1}{24} c_1 c_2 t^3 - \frac{1}{720} (c_1^4 - 4 c_1^2 c_2 - 3 c_2^2 - c_1 c_3 + c_4) t^4 + \frac{(-c_1^3 c_2 + 3 c_1 c_2^2 + c_1^2 c_3 - c_1 c_4) t^5}{1440} + \frac{(c_1^6 - 6 c_1^4 c_2 + \frac{11 c_1^2 c_2^2}{2} + 5 c_2^3 + \frac{5 c_1^3 c_3}{2} + \frac{11 c_1 c_2 c_3}{2} - \frac{c_3^2}{2} - \frac{5 c_1^2 c_4}{2} - \frac{9 c_2 c_4}{2} - c_1 c_5 + c_6) t^6}{30240}$$

In[2]:= **AugmentedSymmetricPolynomial**[{6}, {a, b, c, d, e, f, g, h, i, j}]

$$\text{Out[2]= } a^6 + b^6 + c^6 + d^6 + e^6 + f^6 + g^6 + h^6 + i^6 + j^6$$

In[3]:= **SymmetricReduction**[%2, {a, b, c, d, e, f, g, h, i, j}, {d1, d2, d3, d4, d5, d6, d7, d8, d9, d10}]

$$\text{Out[3]= } \{d_1^6 - 6 d_1^4 d_2 + 9 d_1^2 d_2^2 - 2 d_2^3 + 6 d_1^3 d_3 - 12 d_1 d_2 d_3 + 3 d_3^2 - 6 d_1^2 d_4 + 6 d_2 d_4 + 6 d_1 d_5 - 6 d_6, 0\}$$

In[4]:= **s6 = First**[%3]

$$\text{Out[4]= } d_1^6 - 6 d_1^4 d_2 + 9 d_1^2 d_2^2 - 2 d_2^3 + 6 d_1^3 d_3 - 12 d_1 d_2 d_3 + 3 d_3^2 - 6 d_1^2 d_4 + 6 d_2 d_4 + 6 d_1 d_5 - 6 d_6$$

In[5]:= **AugmentedSymmetricPolynomial**[{5}, {a, b, c, d, e, f, g, h, i, j}]

$$\text{Out[5]= } a^5 + b^5 + c^5 + d^5 + e^5 + f^5 + g^5 + h^5 + i^5 + j^5$$

In[6]:= **SymmetricReduction**[%5, {a, b, c, d, e, f, g, h, i, j}, {d1, d2, d3, d4, d5, d6, d7, d8, d9, d10}]

$$\text{Out[6]= } \{d_1^5 - 5 d_1^3 d_2 + 5 d_1 d_2^2 + 5 d_1^2 d_3 - 5 d_2 d_3 - 5 d_1 d_4 + 5 d_5, 0\}$$

In[7]:= **s5 = First**[%6]

$$\text{Out[7]= } d_1^5 - 5 d_1^3 d_2 + 5 d_1 d_2^2 + 5 d_1^2 d_3 - 5 d_2 d_3 - 5 d_1 d_4 + 5 d_5$$

$$\text{In[8]:= ch} = 10 + d1 * t + (1/2) * (d1^2 - 2 * d2) * t^2 + (1/6) * (d1^3 - 3 * d1 * d2 + 3 * d3) * t^3 + \\ (1/24) * (d1^4 - 4 * d1^2 * d2 + 4 * d1 * d3 + 2 * d2^2 - 4 * d4) * t^4 + \\ (1/120) * s5 * t^5 + (1/720) * s6 * t^6$$

$$\text{Out[8]= } 10 + d1 t + \frac{1}{2} (d1^2 - 2 d2) t^2 + \frac{1}{6} (d1^3 - 3 d1 d2 + 3 d3) t^3 + \\ \frac{1}{24} (d1^4 - 4 d1^2 d2 + 2 d2^2 + 4 d1 d3 - 4 d4) t^4 + \\ \frac{1}{120} (d1^5 - 5 d1^3 d2 + 5 d1 d2^2 + 5 d1^2 d3 - 5 d2 d3 - 5 d1 d4 + 5 d5) t^5 + \\ \frac{1}{720} (d1^6 - 6 d1^4 d2 + 9 d1^2 d2^2 - 2 d2^3 + 6 d1^3 d3 - \\ 12 d1 d2 d3 + 3 d3^2 - 6 d1^2 d4 + 6 d2 d4 + 6 d1 d5 - 6 d6) t^6$$

$$\text{In[9]:= Expand[ch * td]}$$

$$\text{Out[9]= } 10 + 5 c1 t + d1 t + \frac{5 c1^2 t^2}{6} + \frac{5 c2 t^2}{6} + \frac{1}{2} c1 d1 t^2 + \frac{d1^2 t^2}{2} - d2 t^2 + \frac{5}{12} c1 c2 t^3 + \\ \frac{1}{12} c1^2 d1 t^3 + \frac{1}{12} c2 d1 t^3 + \frac{1}{4} c1 d1^2 t^3 + \frac{d1^3 t^3}{6} - \frac{1}{2} c1 d2 t^3 - \frac{1}{2} d1 d2 t^3 + \frac{d3 t^3}{2} - \\ \frac{c1^4 t^4}{72} + \frac{1}{18} c1^2 c2 t^4 + \frac{c2^2 t^4}{24} + \frac{1}{72} c1 c3 t^4 - \frac{c4 t^4}{72} + \frac{1}{24} c1 c2 d1 t^4 + \frac{1}{24} c1^2 d1^2 t^4 + \\ \frac{1}{24} c2 d1^2 t^4 + \frac{1}{12} c1 d1^3 t^4 + \frac{d1^4 t^4}{24} - \frac{1}{12} c1^2 d2 t^4 - \frac{1}{12} c2 d2 t^4 - \frac{1}{4} c1 d1 d2 t^4 - \\ \frac{1}{6} d1^2 d2 t^4 + \frac{d2^2 t^4}{12} + \frac{1}{4} c1 d3 t^4 + \frac{1}{6} d1 d3 t^4 - \frac{d4 t^4}{6} - \frac{1}{144} c1^3 c2 t^5 + \frac{1}{48} c1 c2^2 t^5 + \\ \frac{1}{144} c1^2 c3 t^5 - \frac{1}{144} c1 c4 t^5 - \frac{1}{720} c1^4 d1 t^5 + \frac{1}{180} c1^2 c2 d1 t^5 + \frac{1}{240} c2^2 d1 t^5 + \\ \frac{1}{720} c1 c3 d1 t^5 - \frac{1}{720} c4 d1 t^5 + \frac{1}{48} c1 c2 d1^2 t^5 + \frac{1}{72} c1^2 d1^3 t^5 + \frac{1}{72} c2 d1^3 t^5 + \\ \frac{1}{48} c1 d1^4 t^5 + \frac{d1^5 t^5}{120} - \frac{1}{24} c1 c2 d2 t^5 - \frac{1}{24} c1^2 d1 d2 t^5 - \frac{1}{24} c2 d1 d2 t^5 - \frac{1}{12} c1 d1^2 d2 t^5 - \\ \frac{1}{24} d1^3 d2 t^5 + \frac{1}{24} c1 d2^2 t^5 + \frac{1}{24} d1 d2^2 t^5 + \frac{1}{24} c1^2 d3 t^5 + \frac{1}{24} c2 d3 t^5 + \frac{1}{12} c1 d1 d3 t^5 + \\ \frac{1}{24} d1^2 d3 t^5 - \frac{1}{24} d2 d3 t^5 - \frac{1}{12} c1 d4 t^5 - \frac{1}{24} d1 d4 t^5 + \frac{d5 t^5}{24} + \frac{c1^6 t^6}{3024} - \frac{1}{504} c1^4 c2 t^6 + \\ \frac{11 c1^2 c2^2 t^6}{6048} + \frac{5 c2^3 t^6}{3024} + \frac{5 c1^3 c3 t^6}{6048} + \frac{11 c1 c2 c3 t^6}{6048} - \frac{c3^2 t^6}{6048} - \frac{5 c1^2 c4 t^6}{6048} - \\ \frac{1}{672} c2 c4 t^6 - \frac{c1 c5 t^6}{3024} + \frac{c6 t^6}{3024} - \frac{c1^3 c2 d1 t^6}{1440} + \frac{1}{480} c1 c2^2 d1 t^6 + \frac{c1^2 c3 d1 t^6}{1440} - \\ \frac{c1 c4 d1 t^6}{1440} - \frac{c1^4 d1^2 t^6}{1440} + \frac{1}{360} c1^2 c2 d1^2 t^6 + \frac{1}{480} c2^2 d1^2 t^6 + \frac{c1 c3 d1^2 t^6}{1440} - \\ \frac{c4 d1^2 t^6}{1440} + \frac{1}{144} c1 c2 d1^3 t^6 + \frac{1}{288} c1^2 d1^4 t^6 + \frac{1}{288} c2 d1^4 t^6 + \frac{1}{240} c1 d1^5 t^6 + \frac{d1^6 t^6}{720} + \\ \frac{1}{720} c1^4 d2 t^6 - \frac{1}{180} c1^2 c2 d2 t^6 - \frac{1}{240} c2^2 d2 t^6 - \frac{1}{720} c1 c3 d2 t^6 + \frac{1}{720} c4 d2 t^6 - \\ \frac{1}{48} c1 c2 d1 d2 t^6 - \frac{1}{72} c1^2 d1^2 d2 t^6 - \frac{1}{72} c2 d1^2 d2 t^6 - \frac{1}{48} c1 d1^3 d2 t^6 - \frac{1}{120} d1^4 d2 t^6 +$$

$$\begin{aligned}
& \frac{1}{144} c_1^2 d_2^2 t^6 + \frac{1}{144} c_2 d_2^2 t^6 + \frac{1}{48} c_1 d_1 d_2^2 t^6 + \frac{1}{80} d_1^2 d_2^2 t^6 - \frac{d_2^3 t^6}{360} + \frac{1}{48} c_1 c_2 d_3 t^6 + \\
& \frac{1}{72} c_1^2 d_1 d_3 t^6 + \frac{1}{72} c_2 d_1 d_3 t^6 + \frac{1}{48} c_1 d_1^2 d_3 t^6 + \frac{1}{120} d_1^3 d_3 t^6 - \frac{1}{48} c_1 d_2 d_3 t^6 - \\
& \frac{1}{60} d_1 d_2 d_3 t^6 + \frac{d_3^2 t^6}{240} - \frac{1}{72} c_1^2 d_4 t^6 - \frac{1}{72} c_2 d_4 t^6 - \frac{1}{48} c_1 d_1 d_4 t^6 - \frac{1}{120} d_1^2 d_4 t^6 + \\
& \frac{1}{120} d_2 d_4 t^6 + \frac{1}{48} c_1 d_5 t^6 + \frac{1}{120} d_1 d_5 t^6 - \frac{d_6 t^6}{120} + \frac{c_1^6 d_1 t^7}{30240} - \frac{c_1^4 c_2 d_1 t^7}{5040} + \\
& \frac{11 c_1^2 c_2^2 d_1 t^7}{60480} + \frac{c_2^3 d_1 t^7}{6048} + \frac{c_1^3 c_3 d_1 t^7}{12096} + \frac{11 c_1 c_2 c_3 d_1 t^7}{60480} - \frac{c_3^2 d_1 t^7}{60480} - \\
& \frac{c_1^2 c_4 d_1 t^7}{12096} - \frac{c_2 c_4 d_1 t^7}{6720} - \frac{c_1 c_5 d_1 t^7}{30240} + \frac{c_6 d_1 t^7}{30240} - \frac{c_1^3 c_2 d_1^2 t^7}{2880} + \frac{1}{960} c_1 c_2^2 d_1^2 t^7 + \\
& \frac{c_1^2 c_3 d_1^2 t^7}{2880} - \frac{c_1 c_4 d_1^2 t^7}{2880} - \frac{c_1^4 d_1^3 t^7}{4320} + \frac{c_1^2 c_2 d_1^3 t^7}{1080} + \frac{c_2^2 d_1^3 t^7}{1440} + \frac{c_1 c_3 d_1^3 t^7}{4320} - \\
& \frac{c_4 d_1^3 t^7}{4320} + \frac{1}{576} c_1 c_2 d_1^4 t^7 + \frac{c_1^2 d_1^5 t^7}{1440} + \frac{c_2 d_1^5 t^7}{1440} + \frac{c_1 d_1^6 t^7}{1440} + \frac{c_1^3 c_2 d_2 t^7}{1440} - \\
& \frac{1}{480} c_1 c_2^2 d_2 t^7 - \frac{c_1^2 c_3 d_2 t^7}{1440} + \frac{c_1 c_4 d_2 t^7}{1440} + \frac{c_1^4 d_1 d_2 t^7}{1440} - \frac{1}{360} c_1^2 c_2 d_1 d_2 t^7 - \\
& \frac{1}{480} c_2^2 d_1 d_2 t^7 - \frac{c_1 c_3 d_1 d_2 t^7}{1440} + \frac{c_4 d_1 d_2 t^7}{1440} - \frac{1}{144} c_1 c_2 d_1^2 d_2 t^7 - \frac{1}{288} c_1^2 d_1^3 d_2 t^7 - \\
& \frac{1}{288} c_2 d_1^3 d_2 t^7 - \frac{1}{240} c_1 d_1^4 d_2 t^7 + \frac{1}{288} c_1 c_2 d_2^2 t^7 + \frac{1}{288} c_1^2 d_1 d_2^2 t^7 + \\
& \frac{1}{288} c_2 d_1 d_2^2 t^7 + \frac{1}{160} c_1 d_1^2 d_2^2 t^7 - \frac{1}{720} c_1 d_2^3 t^7 - \frac{c_1^4 d_3 t^7}{1440} + \frac{1}{360} c_1^2 c_2 d_3 t^7 + \\
& \frac{1}{480} c_2^2 d_3 t^7 + \frac{c_1 c_3 d_3 t^7}{1440} - \frac{c_4 d_3 t^7}{1440} + \frac{1}{144} c_1 c_2 d_1 d_3 t^7 + \frac{1}{288} c_1^2 d_1^2 d_3 t^7 + \\
& \frac{1}{288} c_2 d_1^2 d_3 t^7 + \frac{1}{240} c_1 d_1^3 d_3 t^7 - \frac{1}{288} c_1^2 d_2 d_3 t^7 - \frac{1}{288} c_2 d_2 d_3 t^7 - \\
& \frac{1}{120} c_1 d_1 d_2 d_3 t^7 + \frac{1}{480} c_1 d_3^2 t^7 - \frac{1}{144} c_1 c_2 d_4 t^7 - \frac{1}{288} c_1^2 d_1 d_4 t^7 - \frac{1}{288} c_2 d_1 d_4 t^7 - \\
& \frac{1}{240} c_1 d_1^2 d_4 t^7 + \frac{1}{240} c_1 d_2 d_4 t^7 + \frac{1}{288} c_1^2 d_5 t^7 + \frac{1}{288} c_2 d_5 t^7 + \frac{1}{240} c_1 d_1 d_5 t^7 - \\
& \frac{1}{240} c_1 d_6 t^7 + \frac{c_1^6 d_1^2 t^8}{60480} - \frac{c_1^4 c_2 d_1^2 t^8}{10080} + \frac{11 c_1^2 c_2^2 d_1^2 t^8}{120960} + \frac{c_2^3 d_1^2 t^8}{12096} + \\
& \frac{c_1^3 c_3 d_1^2 t^8}{24192} + \frac{11 c_1 c_2 c_3 d_1^2 t^8}{120960} - \frac{c_3^2 d_1^2 t^8}{120960} - \frac{c_1^2 c_4 d_1^2 t^8}{24192} - \frac{c_2 c_4 d_1^2 t^8}{13440} - \\
& \frac{c_1^4 d_1^4 t^8}{17280} + \frac{c_1^2 c_2 d_1^4 t^8}{4320} + \frac{c_2^2 d_1^4 t^8}{5760} + \frac{c_1 c_3 d_1^4 t^8}{17280} - \frac{c_4 d_1^4 t^8}{17280} + \frac{c_1 c_2 d_1^5 t^8}{2880} + \\
& \frac{c_1^2 d_1^6 t^8}{8640} + \frac{c_2 d_1^6 t^8}{8640} - \frac{c_1^6 d_2 t^8}{30240} + \frac{c_1^4 c_2 d_2 t^8}{5040} - \frac{11 c_1^2 c_2^2 d_2 t^8}{60480} - \frac{c_2^3 d_2 t^8}{6048} - \\
& \frac{c_1^3 c_3 d_2 t^8}{12096} - \frac{11 c_1 c_2 c_3 d_2 t^8}{60480} + \frac{c_3^2 d_2 t^8}{60480} + \frac{c_1^2 c_4 d_2 t^8}{12096} + \frac{c_2 c_4 d_2 t^8}{6720} + \frac{c_1 c_5 d_2 t^8}{30240} -
\end{aligned}$$

$$\begin{aligned}
& \frac{c_6 d_2 t^8}{30240} + \frac{c_1^3 c_2 d_1 d_2 t^8}{2880} - \frac{1}{960} c_1 c_2^2 d_1 d_2 t^8 - \frac{c_1^2 c_3 d_1 d_2 t^8}{2880} + \frac{c_1 c_4 d_1 d_2 t^8}{2880} + \\
& \frac{c_1^4 d_1^2 d_2 t^8}{4320} - \frac{c_1^2 c_2 d_1^2 d_2 t^8}{1080} - \frac{c_2^2 d_1^2 d_2 t^8}{1440} - \frac{c_1 c_3 d_1^2 d_2 t^8}{4320} + \frac{c_4 d_1^2 d_2 t^8}{4320} - \\
& \frac{1}{576} c_1 c_2 d_1^3 d_2 t^8 - \frac{c_1^2 d_1^4 d_2 t^8}{1440} - \frac{c_2 d_1^4 d_2 t^8}{1440} - \frac{c_1^4 d_2^2 t^8}{8640} + \frac{c_1^2 c_2 d_2^2 t^8}{2160} + \\
& \frac{c_2^2 d_2^2 t^8}{2880} + \frac{c_1 c_3 d_2^2 t^8}{8640} - \frac{c_4 d_2^2 t^8}{8640} + \frac{1}{576} c_1 c_2 d_1 d_2^2 t^8 + \frac{1}{960} c_1^2 d_1^2 d_2^2 t^8 + \\
& \frac{1}{960} c_2 d_1^2 d_2^2 t^8 - \frac{c_1^2 d_2^3 t^8}{4320} - \frac{c_2 d_2^3 t^8}{4320} - \frac{c_1^3 c_2 d_3 t^8}{2880} + \frac{1}{960} c_1 c_2^2 d_3 t^8 + \\
& \frac{c_1^2 c_3 d_3 t^8}{2880} - \frac{c_1 c_4 d_3 t^8}{2880} - \frac{c_1^4 d_1 d_3 t^8}{4320} + \frac{c_1^2 c_2 d_1 d_3 t^8}{1080} + \frac{c_2^2 d_1 d_3 t^8}{1440} + \\
& \frac{c_1 c_3 d_1 d_3 t^8}{4320} - \frac{c_4 d_1 d_3 t^8}{4320} + \frac{1}{576} c_1 c_2 d_1^2 d_3 t^8 + \frac{c_1^2 d_1^3 d_3 t^8}{1440} + \frac{c_2 d_1^3 d_3 t^8}{1440} - \\
& \frac{1}{576} c_1 c_2 d_2 d_3 t^8 - \frac{1}{720} c_1^2 d_1 d_2 d_3 t^8 - \frac{1}{720} c_2 d_1 d_2 d_3 t^8 + \frac{c_1^2 d_3^2 t^8}{2880} + \frac{c_2 d_3^2 t^8}{2880} + \\
& \frac{c_1^4 d_4 t^8}{4320} - \frac{c_1^2 c_2 d_4 t^8}{1080} - \frac{c_2^2 d_4 t^8}{1440} - \frac{c_1 c_3 d_4 t^8}{4320} + \frac{c_4 d_4 t^8}{4320} - \frac{1}{576} c_1 c_2 d_1 d_4 t^8 - \\
& \frac{c_1^2 d_1^2 d_4 t^8}{1440} - \frac{c_2 d_1^2 d_4 t^8}{1440} + \frac{c_1^2 d_2 d_4 t^8}{1440} + \frac{c_2 d_2 d_4 t^8}{1440} + \frac{1}{576} c_1 c_2 d_5 t^8 + \\
& \frac{c_1^2 d_1 d_5 t^8}{1440} + \frac{c_2 d_1 d_5 t^8}{1440} - \frac{c_1^2 d_6 t^8}{1440} - \frac{c_2 d_6 t^8}{1440} + \frac{c_1^6 d_1^3 t^9}{181440} - \frac{c_1^4 c_2 d_1^3 t^9}{30240} + \\
& \frac{11 c_1^2 c_2^2 d_1^3 t^9}{362880} + \frac{c_2^3 d_1^3 t^9}{36288} + \frac{c_1^3 c_3 d_1^3 t^9}{72576} + \frac{11 c_1 c_2 c_3 d_1^3 t^9}{362880} - \frac{c_3^2 d_1^3 t^9}{362880} - \\
& \frac{c_1^2 c_4 d_1^3 t^9}{72576} - \frac{c_2 c_4 d_1^3 t^9}{40320} - \frac{c_1 c_5 d_1^3 t^9}{181440} + \frac{c_6 d_1^3 t^9}{181440} - \frac{c_1^3 c_2 d_1^4 t^9}{34560} + \frac{c_1 c_2^2 d_1^4 t^9}{11520} + \\
& \frac{c_1^2 c_3 d_1^4 t^9}{34560} - \frac{c_1 c_4 d_1^4 t^9}{34560} - \frac{c_1^4 d_1^5 t^9}{86400} + \frac{c_1^2 c_2 d_1^5 t^9}{21600} + \frac{c_2^2 d_1^5 t^9}{28800} + \frac{c_1 c_3 d_1^5 t^9}{86400} - \\
& \frac{c_4 d_1^5 t^9}{86400} + \frac{c_1 c_2 d_1^6 t^9}{17280} - \frac{c_1^6 d_1 d_2 t^9}{60480} + \frac{c_1^4 c_2 d_1 d_2 t^9}{10080} - \frac{11 c_1^2 c_2^2 d_1 d_2 t^9}{120960} - \\
& \frac{c_2^3 d_1 d_2 t^9}{12096} - \frac{c_1^3 c_3 d_1 d_2 t^9}{24192} - \frac{11 c_1 c_2 c_3 d_1 d_2 t^9}{120960} + \frac{c_3^2 d_1 d_2 t^9}{120960} + \frac{c_1^2 c_4 d_1 d_2 t^9}{24192} + \\
& \frac{c_2 c_4 d_1 d_2 t^9}{13440} + \frac{c_1 c_5 d_1 d_2 t^9}{60480} - \frac{c_6 d_1 d_2 t^9}{60480} + \frac{c_1^3 c_2 d_1^2 d_2 t^9}{8640} - \frac{c_1 c_2^2 d_1^2 d_2 t^9}{2880} - \\
& \frac{c_1^2 c_3 d_1^2 d_2 t^9}{8640} + \frac{c_1 c_4 d_1^2 d_2 t^9}{8640} + \frac{c_1^4 d_1^3 d_2 t^9}{17280} - \frac{c_1^2 c_2 d_1^3 d_2 t^9}{4320} - \frac{c_2^2 d_1^3 d_2 t^9}{5760} - \\
& \frac{c_1 c_3 d_1^3 d_2 t^9}{17280} + \frac{c_4 d_1^3 d_2 t^9}{17280} - \frac{c_1 c_2 d_1^4 d_2 t^9}{2880} - \frac{c_1^3 c_2 d_2^2 t^9}{17280} + \frac{c_1 c_2^2 d_2^2 t^9}{5760} + \\
& \frac{c_1^2 c_3 d_2^2 t^9}{17280} - \frac{c_1 c_4 d_2^2 t^9}{17280} - \frac{c_1^4 d_1 d_2^2 t^9}{17280} + \frac{c_1^2 c_2 d_1 d_2^2 t^9}{4320} + \frac{c_2^2 d_1 d_2^2 t^9}{5760} + \\
& \frac{c_1 c_3 d_1 d_2^2 t^9}{17280} - \frac{c_4 d_1 d_2^2 t^9}{17280} + \frac{c_1 c_2 d_1^2 d_2^2 t^9}{1920} - \frac{c_1 c_2 d_2^3 t^9}{8640} + \frac{c_1^6 d_3 t^9}{60480} - \\
& \frac{c_1^4 c_2 d_3 t^9}{10080} + \frac{11 c_1^2 c_2^2 d_3 t^9}{120960} + \frac{c_2^3 d_3 t^9}{12096} + \frac{c_1^3 c_3 d_3 t^9}{24192} + \frac{11 c_1 c_2 c_3 d_3 t^9}{120960} -
\end{aligned}$$

$$\begin{aligned}
& \frac{c^3 d^3 t^9}{120960} - \frac{c^1 c^4 d^3 t^9}{24192} - \frac{c^2 c^4 d^3 t^9}{13440} - \frac{c^1 c^5 d^3 t^9}{60480} + \frac{c^6 d^3 t^9}{60480} - \frac{c^1 c^3 c^2 d^1 d^3 t^9}{8640} + \\
& \frac{c^1 c^2 d^1 d^3 t^9}{2880} + \frac{c^1 c^3 d^1 d^3 t^9}{8640} - \frac{c^1 c^4 d^1 d^3 t^9}{8640} - \frac{c^1 c^4 d^1 d^3 t^9}{17280} + \frac{c^1 c^2 d^1 d^3 t^9}{4320} + \\
& \frac{c^2 d^1 d^2 d^3 t^9}{5760} + \frac{c^1 c^3 d^1 d^2 d^3 t^9}{17280} - \frac{c^4 d^1 d^2 d^3 t^9}{17280} + \frac{c^1 c^2 d^1 d^3 d^3 t^9}{2880} + \frac{c^1 c^4 d^2 d^3 t^9}{17280} - \\
& \frac{c^1 c^2 c^2 d^2 d^3 t^9}{4320} - \frac{c^2 c^2 d^2 d^3 t^9}{5760} - \frac{c^1 c^3 c^2 d^2 d^3 t^9}{17280} + \frac{c^4 d^2 d^3 t^9}{17280} - \frac{c^1 c^2 d^1 d^2 d^3 t^9}{1440} + \\
& \frac{c^1 c^2 d^3 t^9}{5760} + \frac{c^1 c^3 c^2 d^4 t^9}{8640} - \frac{c^1 c^2 c^2 d^4 t^9}{2880} - \frac{c^1 c^2 c^3 d^4 t^9}{8640} + \frac{c^1 c^4 d^4 t^9}{8640} + \frac{c^1 c^4 d^1 d^4 t^9}{17280} - \\
& \frac{c^1 c^2 c^2 d^1 d^4 t^9}{4320} - \frac{c^2 c^2 d^1 d^4 t^9}{5760} - \frac{c^1 c^3 c^2 d^1 d^4 t^9}{17280} + \frac{c^4 d^1 d^4 t^9}{17280} - \frac{c^1 c^2 d^1 d^2 d^4 t^9}{2880} + \\
& \frac{c^1 c^2 d^2 d^4 t^9}{2880} - \frac{c^1 c^4 d^5 t^9}{17280} + \frac{c^1 c^2 c^2 d^5 t^9}{4320} + \frac{c^2 c^2 d^5 t^9}{5760} + \frac{c^1 c^3 c^2 d^5 t^9}{17280} - \frac{c^4 d^5 t^9}{17280} + \\
& \frac{c^1 c^2 d^1 d^5 t^9}{2880} - \frac{c^1 c^2 d^6 t^9}{2880} + \frac{c^1 c^6 d^1 d^4 t^{10}}{725760} - \frac{c^1 c^4 c^2 d^1 d^4 t^{10}}{120960} + \frac{11 c^1 c^2 c^2 d^1 d^4 t^{10}}{1451520} + \\
& \frac{c^2 c^3 d^1 d^4 t^{10}}{145152} + \frac{c^1 c^3 c^3 d^1 d^4 t^{10}}{290304} + \frac{11 c^1 c^1 c^2 c^3 d^1 d^4 t^{10}}{1451520} - \frac{c^3 c^2 d^1 d^4 t^{10}}{1451520} - \frac{c^1 c^2 c^4 d^1 d^4 t^{10}}{290304} - \\
& \frac{c^2 c^4 d^1 d^4 t^{10}}{161280} - \frac{c^1 c^5 d^1 d^4 t^{10}}{725760} + \frac{c^6 d^1 d^4 t^{10}}{725760} - \frac{c^1 c^3 c^2 d^1 d^5 t^{10}}{172800} + \frac{c^1 c^2 c^2 d^1 d^5 t^{10}}{57600} + \\
& \frac{c^1 c^2 c^3 d^1 d^5 t^{10}}{172800} - \frac{c^1 c^4 d^1 d^5 t^{10}}{172800} - \frac{c^1 c^4 d^1 d^6 t^{10}}{518400} + \frac{c^1 c^2 c^2 d^1 d^6 t^{10}}{129600} + \frac{c^2 c^2 d^1 d^6 t^{10}}{172800} + \frac{c^1 c^3 c^2 d^1 d^6 t^{10}}{518400} - \\
& \frac{c^4 d^1 d^6 t^{10}}{518400} - \frac{c^1 c^6 d^1 d^2 d^2 t^{10}}{181440} + \frac{c^1 c^4 c^2 d^1 d^2 d^2 t^{10}}{30240} - \frac{11 c^1 c^2 c^2 d^1 d^2 d^2 t^{10}}{362880} - \frac{c^2 c^3 d^1 d^2 d^2 t^{10}}{36288} - \\
& \frac{c^1 c^3 c^3 d^1 d^2 d^2 t^{10}}{72576} - \frac{11 c^1 c^1 c^2 c^3 d^1 d^2 d^2 t^{10}}{362880} + \frac{c^3 c^2 d^1 d^2 d^2 t^{10}}{362880} + \frac{c^1 c^2 c^4 d^1 d^2 d^2 t^{10}}{72576} + \\
& \frac{c^2 c^4 d^1 d^2 d^2 t^{10}}{40320} + \frac{c^1 c^5 d^1 d^2 d^2 t^{10}}{181440} - \frac{c^6 d^1 d^2 d^2 t^{10}}{181440} + \frac{c^1 c^3 c^2 d^1 d^3 d^2 t^{10}}{34560} - \frac{c^1 c^2 c^2 d^1 d^3 d^2 t^{10}}{11520} - \\
& \frac{c^1 c^2 c^3 d^1 d^3 d^2 t^{10}}{34560} + \frac{c^1 c^4 d^1 d^3 d^2 t^{10}}{34560} + \frac{c^1 c^4 d^1 d^4 d^2 t^{10}}{86400} - \frac{c^1 c^2 c^2 d^1 d^4 d^2 t^{10}}{21600} - \frac{c^2 c^2 d^1 d^4 d^2 t^{10}}{28800} - \\
& \frac{c^1 c^3 d^1 d^4 d^2 t^{10}}{86400} + \frac{c^4 d^1 d^4 d^2 t^{10}}{86400} + \frac{c^1 c^6 d^2 d^2 t^{10}}{362880} - \frac{c^1 c^4 c^2 d^2 d^2 t^{10}}{60480} + \frac{11 c^1 c^2 c^2 d^2 d^2 t^{10}}{725760} + \\
& \frac{c^2 c^3 d^2 d^2 t^{10}}{72576} + \frac{c^1 c^3 c^3 d^2 d^2 t^{10}}{145152} + \frac{11 c^1 c^1 c^2 c^3 d^2 d^2 t^{10}}{725760} - \frac{c^3 c^2 d^2 d^2 t^{10}}{725760} - \frac{c^1 c^2 c^4 d^2 d^2 t^{10}}{145152} - \\
& \frac{c^2 c^4 d^2 d^2 t^{10}}{80640} - \frac{c^1 c^5 d^2 d^2 t^{10}}{362880} + \frac{c^6 d^2 d^2 t^{10}}{362880} - \frac{c^1 c^3 c^2 d^1 d^2 d^2 t^{10}}{34560} + \frac{c^1 c^2 c^2 d^1 d^2 d^2 t^{10}}{11520} + \\
& \frac{c^1 c^2 c^3 d^1 d^2 d^2 t^{10}}{34560} - \frac{c^1 c^4 d^1 d^2 d^2 t^{10}}{34560} - \frac{c^1 c^4 d^1 d^2 d^2 t^{10}}{57600} + \frac{c^1 c^2 c^2 d^1 d^2 d^2 t^{10}}{14400} + \\
& \frac{c^2 c^2 d^1 d^2 d^2 t^{10}}{19200} + \frac{c^1 c^3 d^1 d^2 d^2 t^{10}}{57600} - \frac{c^4 d^1 d^2 d^2 t^{10}}{57600} + \frac{c^1 c^6 d^1 d^3 t^{10}}{259200} - \frac{c^1 c^4 c^2 d^1 d^3 t^{10}}{64800} - \\
& \frac{c^2 c^2 d^3 t^{10}}{86400} - \frac{c^1 c^3 d^2 c^3 t^{10}}{259200} + \frac{c^4 d^2 c^3 t^{10}}{259200} + \frac{c^1 c^6 d^1 d^3 t^{10}}{181440} - \frac{c^1 c^4 c^2 d^1 d^3 t^{10}}{30240} + \\
& \frac{11 c^1 c^2 c^2 d^1 d^3 t^{10}}{362880} + \frac{c^2 c^3 d^1 d^3 t^{10}}{36288} + \frac{c^1 c^3 c^3 d^1 d^3 t^{10}}{72576} + \frac{11 c^1 c^1 c^2 c^3 d^1 d^3 t^{10}}{362880} -
\end{aligned}$$

$$\begin{array}{r}
\frac{c_3^2 d_1 d_3 t^{10}}{362880} - \frac{c_1^2 c_4 d_1 d_3 t^{10}}{72576} - \frac{c_2 c_4 d_1 d_3 t^{10}}{40320} - \frac{c_1 c_5 d_1 d_3 t^{10}}{181440} + \frac{c_6 d_1 d_3 t^{10}}{181440} - \\
\frac{c_1^3 c_2 d_1^2 d_3 t^{10}}{34560} + \frac{c_1 c_2^2 d_1^2 d_3 t^{10}}{11520} + \frac{c_1^2 c_3 d_1^2 d_3 t^{10}}{34560} - \frac{c_1 c_4 d_1^2 d_3 t^{10}}{34560} - \\
\frac{c_1^4 d_1^3 d_3 t^{10}}{86400} + \frac{c_1^2 c_2 d_1^3 d_3 t^{10}}{21600} + \frac{c_2^2 d_1^3 d_3 t^{10}}{28800} + \frac{c_1 c_3 d_1^3 d_3 t^{10}}{86400} - \frac{c_4 d_1^3 d_3 t^{10}}{86400} + \\
\frac{c_1^3 c_2 d_2 d_3 t^{10}}{34560} - \frac{c_1 c_2^2 d_2 d_3 t^{10}}{11520} - \frac{c_1^2 c_3 d_2 d_3 t^{10}}{34560} + \frac{c_1 c_4 d_2 d_3 t^{10}}{34560} + \frac{c_1^4 d_1 d_2 d_3 t^{10}}{43200} - \\
\frac{c_1^2 c_2 d_1 d_2 d_3 t^{10}}{10800} - \frac{c_2^2 d_1 d_2 d_3 t^{10}}{14400} - \frac{c_1 c_3 d_1 d_2 d_3 t^{10}}{43200} + \frac{c_4 d_1 d_2 d_3 t^{10}}{43200} - \\
\frac{c_1^4 d_3^2 t^{10}}{172800} + \frac{c_1^2 c_2 d_3^2 t^{10}}{43200} + \frac{c_2^2 d_3^2 t^{10}}{57600} + \frac{c_1 c_3 d_3^2 t^{10}}{172800} - \frac{c_4 d_3^2 t^{10}}{172800} - \frac{c_1^6 d_4 t^{10}}{181440} + \\
\frac{c_1^4 c_2 d_4 t^{10}}{30240} - \frac{11 c_1^2 c_2^2 d_4 t^{10}}{362880} - \frac{c_2^3 d_4 t^{10}}{36288} - \frac{c_1^3 c_3 d_4 t^{10}}{72576} - \frac{11 c_1 c_2 c_3 d_4 t^{10}}{362880} + \\
\frac{c_3^2 d_4 t^{10}}{362880} + \frac{c_1^2 c_4 d_4 t^{10}}{72576} + \frac{c_2 c_4 d_4 t^{10}}{40320} + \frac{c_1 c_5 d_4 t^{10}}{181440} - \frac{c_6 d_4 t^{10}}{181440} + \frac{c_1^3 c_2 d_1 d_4 t^{10}}{34560} - \\
\frac{c_1 c_2^2 d_1 d_4 t^{10}}{11520} - \frac{c_1^2 c_3 d_1 d_4 t^{10}}{34560} + \frac{c_1 c_4 d_1 d_4 t^{10}}{34560} + \frac{c_1^4 d_1^2 d_4 t^{10}}{86400} - \frac{c_1^2 c_2 d_1^2 d_4 t^{10}}{21600} - \\
\frac{c_2^2 d_1^2 d_4 t^{10}}{28800} - \frac{c_1 c_3 d_1^2 d_4 t^{10}}{86400} + \frac{c_4 d_1^2 d_4 t^{10}}{86400} - \frac{c_1^4 d_2 d_4 t^{10}}{86400} + \frac{c_1^2 c_2 d_2 d_4 t^{10}}{21600} + \\
\frac{c_2^2 d_2 d_4 t^{10}}{28800} + \frac{c_1 c_3 d_2 d_4 t^{10}}{86400} - \frac{c_4 d_2 d_4 t^{10}}{86400} - \frac{c_1^3 c_2 d_5 t^{10}}{34560} + \frac{c_1 c_2^2 d_5 t^{10}}{11520} + \\
\frac{c_1^2 c_3 d_5 t^{10}}{34560} - \frac{c_1 c_4 d_5 t^{10}}{34560} - \frac{c_1^4 d_1 d_5 t^{10}}{86400} + \frac{c_1^2 c_2 d_1 d_5 t^{10}}{21600} + \frac{c_2^2 d_1 d_5 t^{10}}{28800} + \\
\frac{c_1 c_3 d_1 d_5 t^{10}}{86400} - \frac{c_4 d_1 d_5 t^{10}}{86400} + \frac{c_1^4 d_6 t^{10}}{86400} - \frac{c_1^2 c_2 d_6 t^{10}}{21600} - \frac{c_2^2 d_6 t^{10}}{28800} - \frac{c_1 c_3 d_6 t^{10}}{86400} + \\
\frac{c_4 d_6 t^{10}}{86400} + \frac{c_1^6 d_1^5 t^{11}}{3628800} - \frac{c_1^4 c_2 d_1^5 t^{11}}{604800} + \frac{11 c_1^2 c_2^2 d_1^5 t^{11}}{7257600} + \frac{c_2^3 d_1^5 t^{11}}{725760} + \\
\frac{c_1^3 c_3 d_1^5 t^{11}}{1451520} + \frac{11 c_1 c_2 c_3 d_1^5 t^{11}}{7257600} - \frac{c_3^2 d_1^5 t^{11}}{7257600} - \frac{c_1^2 c_4 d_1^5 t^{11}}{1451520} - \frac{c_2 c_4 d_1^5 t^{11}}{806400} - \\
\frac{c_1 c_5 d_1^5 t^{11}}{3628800} + \frac{c_6 d_1^5 t^{11}}{3628800} - \frac{c_1^3 c_2 d_1^6 t^{11}}{1036800} + \frac{c_1 c_2^2 d_1^6 t^{11}}{345600} + \frac{c_1^2 c_3 d_1^6 t^{11}}{1036800} - \\
\frac{c_1 c_4 d_1^6 t^{11}}{1036800} - \frac{c_1^6 d_1^3 d_2 t^{11}}{725760} + \frac{c_1^4 c_2 d_1^3 d_2 t^{11}}{120960} - \frac{11 c_1^2 c_2^2 d_1^3 d_2 t^{11}}{1451520} - \frac{c_2^3 d_1^3 d_2 t^{11}}{145152} - \\
\frac{c_1^3 c_3 d_1^3 d_2 t^{11}}{290304} - \frac{11 c_1 c_2 c_3 d_1^3 d_2 t^{11}}{1451520} + \frac{c_3^2 d_1^3 d_2 t^{11}}{1451520} + \frac{c_1^2 c_4 d_1^3 d_2 t^{11}}{290304} + \\
\frac{c_2 c_4 d_1^3 d_2 t^{11}}{161280} + \frac{c_1 c_5 d_1^3 d_2 t^{11}}{725760} - \frac{c_6 d_1^3 d_2 t^{11}}{725760} + \frac{c_1^3 c_2 d_1^4 d_2 t^{11}}{172800} - \frac{c_1 c_2^2 d_1^4 d_2 t^{11}}{57600} - \\
\frac{c_1^2 c_3 d_1^4 d_2 t^{11}}{172800} + \frac{c_1 c_4 d_1^4 d_2 t^{11}}{172800} + \frac{c_1^6 d_1 d_2^2 t^{11}}{725760} - \frac{c_1^4 c_2 d_1 d_2^2 t^{11}}{120960} + \\
\frac{11 c_1^2 c_2^2 d_1 d_2^2 t^{11}}{1451520} + \frac{c_2^3 d_1 d_2^2 t^{11}}{145152} + \frac{c_1^3 c_3 d_1 d_2^2 t^{11}}{290304} + \frac{11 c_1 c_2 c_3 d_1 d_2^2 t^{11}}{1451520} - \\
\frac{c_3^2 d_1 d_2^2 t^{11}}{1451520} - \frac{c_1^2 c_4 d_1 d_2^2 t^{11}}{290304} - \frac{c_2 c_4 d_1 d_2^2 t^{11}}{161280} - \frac{c_1 c_5 d_1 d_2^2 t^{11}}{725760} + \frac{c_6 d_1 d_2^2 t^{11}}{725760} -
\end{array}$$

$$\begin{aligned}
& \frac{c1^3 c2 d1^2 d2^2 t^{11}}{115200} + \frac{c1 c2^2 d1^2 d2^2 t^{11}}{38400} + \frac{c1^2 c3 d1^2 d2^2 t^{11}}{115200} - \frac{c1 c4 d1^2 d2^2 t^{11}}{115200} + \\
& \frac{c1^3 c2 d2^3 t^{11}}{518400} - \frac{c1 c2^2 d2^3 t^{11}}{172800} - \frac{c1^2 c3 d2^3 t^{11}}{518400} + \frac{c1 c4 d2^3 t^{11}}{518400} + \frac{c1^6 d1^2 d3 t^{11}}{725760} - \\
& \frac{c1^4 c2 d1^2 d3 t^{11}}{120960} + \frac{11 c1^2 c2^2 d1^2 d3 t^{11}}{1451520} + \frac{c2^3 d1^2 d3 t^{11}}{145152} + \frac{c1^3 c3 d1^2 d3 t^{11}}{290304} + \\
& \frac{11 c1 c2 c3 d1^2 d3 t^{11}}{1451520} - \frac{c3^2 d1^2 d3 t^{11}}{1451520} - \frac{c1^2 c4 d1^2 d3 t^{11}}{290304} - \frac{c2 c4 d1^2 d3 t^{11}}{161280} - \\
& \frac{c1 c5 d1^2 d3 t^{11}}{725760} + \frac{c6 d1^2 d3 t^{11}}{725760} - \frac{c1^3 c2 d1^3 d3 t^{11}}{172800} + \frac{c1 c2^2 d1^3 d3 t^{11}}{57600} + \frac{c1^2 c3 d1^3 d3 t^{11}}{172800} - \\
& \frac{c1 c4 d1^3 d3 t^{11}}{172800} - \frac{c1^6 d2 d3 t^{11}}{725760} + \frac{c1^4 c2 d2 d3 t^{11}}{120960} - \frac{11 c1^2 c2^2 d2 d3 t^{11}}{1451520} - \\
& \frac{c2^3 d2 d3 t^{11}}{145152} - \frac{c1^3 c3 d2 d3 t^{11}}{290304} - \frac{11 c1 c2 c3 d2 d3 t^{11}}{1451520} + \frac{c3^2 d2 d3 t^{11}}{1451520} + \\
& \frac{c1^2 c4 d2 d3 t^{11}}{290304} + \frac{c2 c4 d2 d3 t^{11}}{161280} + \frac{c1 c5 d2 d3 t^{11}}{725760} - \frac{c6 d2 d3 t^{11}}{725760} + \frac{c1^3 c2 d1 d2 d3 t^{11}}{86400} - \\
& \frac{c1 c2^2 d1 d2 d3 t^{11}}{28800} - \frac{c1^2 c3 d1 d2 d3 t^{11}}{86400} + \frac{c1 c4 d1 d2 d3 t^{11}}{86400} - \frac{c1^3 c2 d3^2 t^{11}}{345600} + \\
& \frac{c1 c2^2 d3^2 t^{11}}{115200} + \frac{c1^2 c3 d3^2 t^{11}}{345600} - \frac{c1 c4 d3^2 t^{11}}{345600} - \frac{c1^6 d1 d4 t^{11}}{725760} + \frac{c1^4 c2 d1 d4 t^{11}}{120960} - \\
& \frac{11 c1^2 c2^2 d1 d4 t^{11}}{1451520} - \frac{c2^3 d1 d4 t^{11}}{145152} - \frac{c1^3 c3 d1 d4 t^{11}}{290304} - \frac{11 c1 c2 c3 d1 d4 t^{11}}{1451520} + \\
& \frac{c3^2 d1 d4 t^{11}}{1451520} + \frac{c1^2 c4 d1 d4 t^{11}}{290304} + \frac{c2 c4 d1 d4 t^{11}}{161280} + \frac{c1 c5 d1 d4 t^{11}}{725760} - \frac{c6 d1 d4 t^{11}}{725760} + \\
& \frac{c1^3 c2 d1^2 d4 t^{11}}{172800} - \frac{c1 c2^2 d1^2 d4 t^{11}}{57600} - \frac{c1^2 c3 d1^2 d4 t^{11}}{172800} + \frac{c1 c4 d1^2 d4 t^{11}}{172800} - \\
& \frac{c1^3 c2 d2 d4 t^{11}}{172800} + \frac{c1 c2^2 d2 d4 t^{11}}{57600} + \frac{c1^2 c3 d2 d4 t^{11}}{172800} - \frac{c1 c4 d2 d4 t^{11}}{172800} + \frac{c1^6 d5 t^{11}}{725760} - \\
& \frac{c1^4 c2 d5 t^{11}}{120960} + \frac{11 c1^2 c2^2 d5 t^{11}}{1451520} + \frac{c2^3 d5 t^{11}}{145152} + \frac{c1^3 c3 d5 t^{11}}{290304} + \frac{11 c1 c2 c3 d5 t^{11}}{1451520} - \\
& \frac{c3^2 d5 t^{11}}{1451520} - \frac{c1^2 c4 d5 t^{11}}{290304} - \frac{c2 c4 d5 t^{11}}{161280} - \frac{c1 c5 d5 t^{11}}{725760} + \frac{c6 d5 t^{11}}{725760} - \frac{c1^3 c2 d1 d5 t^{11}}{172800} + \\
& \frac{c1 c2^2 d1 d5 t^{11}}{57600} + \frac{c1^2 c3 d1 d5 t^{11}}{172800} - \frac{c1 c4 d1 d5 t^{11}}{172800} + \frac{c1^3 c2 d6 t^{11}}{172800} - \frac{c1 c2^2 d6 t^{11}}{57600} - \\
& \frac{c1^2 c3 d6 t^{11}}{172800} + \frac{c1 c4 d6 t^{11}}{172800} + \frac{c1^6 d1^6 t^{12}}{21772800} - \frac{c1^4 c2 d1^6 t^{12}}{3628800} + \frac{11 c1^2 c2^2 d1^6 t^{12}}{43545600} + \\
& \frac{c2^3 d1^6 t^{12}}{4354560} + \frac{c1^3 c3 d1^6 t^{12}}{8709120} + \frac{11 c1 c2 c3 d1^6 t^{12}}{43545600} - \frac{c3^2 d1^6 t^{12}}{43545600} - \frac{c1^2 c4 d1^6 t^{12}}{8709120} - \\
& \frac{c2 c4 d1^6 t^{12}}{4838400} - \frac{c1 c5 d1^6 t^{12}}{21772800} + \frac{c6 d1^6 t^{12}}{21772800} - \frac{c1^6 d1^4 d2 t^{12}}{3628800} + \frac{c1^4 c2 d1^4 d2 t^{12}}{604800} - \\
& \frac{11 c1^2 c2^2 d1^4 d2 t^{12}}{7257600} - \frac{c2^3 d1^4 d2 t^{12}}{725760} - \frac{c1^3 c3 d1^4 d2 t^{12}}{1451520} - \frac{11 c1 c2 c3 d1^4 d2 t^{12}}{7257600} + \\
& \frac{c3^2 d1^4 d2 t^{12}}{7257600} + \frac{c1^2 c4 d1^4 d2 t^{12}}{1451520} + \frac{c2 c4 d1^4 d2 t^{12}}{806400} + \frac{c1 c5 d1^4 d2 t^{12}}{3628800} -
\end{aligned}$$

$$\begin{aligned}
& \frac{c_6 d_1^4 d_2 t^{12}}{3628800} + \frac{c_1^6 d_1^2 d_2^2 t^{12}}{2419200} - \frac{c_1^4 c_2 d_1^2 d_2^2 t^{12}}{403200} + \frac{11 c_1^2 c_2^2 d_1^2 d_2^2 t^{12}}{4838400} + \\
& \frac{c_2^3 d_1^2 d_2^2 t^{12}}{483840} + \frac{c_1^3 c_3 d_1^2 d_2^2 t^{12}}{967680} + \frac{11 c_1 c_2 c_3 d_1^2 d_2^2 t^{12}}{4838400} - \frac{c_3^2 d_1^2 d_2^2 t^{12}}{4838400} - \\
& \frac{c_1^2 c_4 d_1^2 d_2^2 t^{12}}{967680} - \frac{c_2 c_4 d_1^2 d_2^2 t^{12}}{537600} - \frac{c_1 c_5 d_1^2 d_2^2 t^{12}}{2419200} + \frac{c_6 d_1^2 d_2^2 t^{12}}{2419200} - \\
& \frac{c_1^6 d_2^3 t^{12}}{10886400} + \frac{c_1^4 c_2 d_2^3 t^{12}}{1814400} - \frac{11 c_1^2 c_2^2 d_2^3 t^{12}}{21772800} - \frac{c_2^3 d_2^3 t^{12}}{2177280} - \frac{c_1^3 c_3 d_2^3 t^{12}}{4354560} - \\
& \frac{11 c_1 c_2 c_3 d_2^3 t^{12}}{21772800} + \frac{c_3^2 d_2^3 t^{12}}{21772800} + \frac{c_1^2 c_4 d_2^3 t^{12}}{4354560} + \frac{c_2 c_4 d_2^3 t^{12}}{2419200} + \frac{c_1 c_5 d_2^3 t^{12}}{10886400} - \\
& \frac{c_6 d_2^3 t^{12}}{10886400} + \frac{c_1^6 d_1^3 d_3 t^{12}}{3628800} - \frac{c_1^4 c_2 d_1^3 d_3 t^{12}}{604800} + \frac{11 c_1^2 c_2^2 d_1^3 d_3 t^{12}}{7257600} + \frac{c_2^3 d_1^3 d_3 t^{12}}{725760} + \\
& \frac{c_1^3 c_3 d_1^3 d_3 t^{12}}{1451520} + \frac{11 c_1 c_2 c_3 d_1^3 d_3 t^{12}}{7257600} - \frac{c_3^2 d_1^3 d_3 t^{12}}{7257600} - \frac{c_1^2 c_4 d_1^3 d_3 t^{12}}{1451520} - \\
& \frac{c_2 c_4 d_1^3 d_3 t^{12}}{806400} - \frac{c_1 c_5 d_1^3 d_3 t^{12}}{3628800} + \frac{c_6 d_1^3 d_3 t^{12}}{3628800} - \frac{c_1^6 d_1 d_2 d_3 t^{12}}{1814400} + \\
& \frac{c_1^4 c_2 d_1 d_2 d_3 t^{12}}{302400} - \frac{11 c_1^2 c_2^2 d_1 d_2 d_3 t^{12}}{3628800} - \frac{c_2^3 d_1 d_2 d_3 t^{12}}{362880} - \frac{c_1^3 c_3 d_1 d_2 d_3 t^{12}}{725760} - \\
& \frac{11 c_1 c_2 c_3 d_1 d_2 d_3 t^{12}}{3628800} + \frac{c_3^2 d_1 d_2 d_3 t^{12}}{3628800} + \frac{c_1^2 c_4 d_1 d_2 d_3 t^{12}}{725760} + \frac{c_2 c_4 d_1 d_2 d_3 t^{12}}{403200} + \\
& \frac{c_1 c_5 d_1 d_2 d_3 t^{12}}{1814400} - \frac{c_6 d_1 d_2 d_3 t^{12}}{1814400} + \frac{c_1^6 d_3^2 t^{12}}{7257600} - \frac{c_1^4 c_2 d_3^2 t^{12}}{1209600} + \frac{11 c_1^2 c_2^2 d_3^2 t^{12}}{14515200} + \\
& \frac{c_2^3 d_3^2 t^{12}}{1451520} + \frac{c_1^3 c_3 d_3^2 t^{12}}{2903040} + \frac{11 c_1 c_2 c_3 d_3^2 t^{12}}{14515200} - \frac{c_3^2 d_3^2 t^{12}}{14515200} - \frac{c_1^2 c_4 d_3^2 t^{12}}{2903040} - \\
& \frac{c_2 c_4 d_3^2 t^{12}}{1612800} - \frac{c_1 c_5 d_3^2 t^{12}}{7257600} + \frac{c_6 d_3^2 t^{12}}{7257600} - \frac{c_1^6 d_1^2 d_4 t^{12}}{3628800} + \frac{c_1^4 c_2 d_1^2 d_4 t^{12}}{604800} - \\
& \frac{11 c_1^2 c_2^2 d_1^2 d_4 t^{12}}{7257600} - \frac{c_2^3 d_1^2 d_4 t^{12}}{725760} - \frac{c_1^3 c_3 d_1^2 d_4 t^{12}}{1451520} - \frac{11 c_1 c_2 c_3 d_1^2 d_4 t^{12}}{7257600} + \\
& \frac{c_3^2 d_1^2 d_4 t^{12}}{7257600} + \frac{c_1^2 c_4 d_1^2 d_4 t^{12}}{1451520} + \frac{c_2 c_4 d_1^2 d_4 t^{12}}{806400} + \frac{c_1 c_5 d_1^2 d_4 t^{12}}{3628800} - \\
& \frac{c_6 d_1^2 d_4 t^{12}}{3628800} + \frac{c_1^6 d_2 d_4 t^{12}}{3628800} - \frac{c_1^4 c_2 d_2 d_4 t^{12}}{604800} + \frac{11 c_1^2 c_2^2 d_2 d_4 t^{12}}{7257600} + \frac{c_2^3 d_2 d_4 t^{12}}{725760} + \\
& \frac{c_1^3 c_3 d_2 d_4 t^{12}}{1451520} + \frac{11 c_1 c_2 c_3 d_2 d_4 t^{12}}{7257600} - \frac{c_3^2 d_2 d_4 t^{12}}{7257600} - \frac{c_1^2 c_4 d_2 d_4 t^{12}}{1451520} - \\
& \frac{c_2 c_4 d_2 d_4 t^{12}}{806400} - \frac{c_1 c_5 d_2 d_4 t^{12}}{3628800} + \frac{c_6 d_2 d_4 t^{12}}{3628800} + \frac{c_1^6 d_1 d_5 t^{12}}{3628800} - \frac{c_1^4 c_2 d_1 d_5 t^{12}}{604800} + \\
& \frac{11 c_1^2 c_2^2 d_1 d_5 t^{12}}{7257600} + \frac{c_2^3 d_1 d_5 t^{12}}{725760} + \frac{c_1^3 c_3 d_1 d_5 t^{12}}{1451520} + \frac{11 c_1 c_2 c_3 d_1 d_5 t^{12}}{7257600} - \\
& \frac{c_3^2 d_1 d_5 t^{12}}{7257600} - \frac{c_1^2 c_4 d_1 d_5 t^{12}}{1451520} - \frac{c_2 c_4 d_1 d_5 t^{12}}{806400} - \frac{c_1 c_5 d_1 d_5 t^{12}}{3628800} + \frac{c_6 d_1 d_5 t^{12}}{3628800} - \\
& \frac{c_1^6 d_6 t^{12}}{3628800} + \frac{c_1^4 c_2 d_6 t^{12}}{604800} - \frac{11 c_1^2 c_2^2 d_6 t^{12}}{7257600} - \frac{c_2^3 d_6 t^{12}}{725760} - \frac{c_1^3 c_3 d_6 t^{12}}{1451520} - \\
& \frac{11 c_1 c_2 c_3 d_6 t^{12}}{7257600} + \frac{c_3^2 d_6 t^{12}}{7257600} + \frac{c_1^2 c_4 d_6 t^{12}}{1451520} + \frac{c_2 c_4 d_6 t^{12}}{806400} + \frac{c_1 c_5 d_6 t^{12}}{3628800} - \frac{c_6 d_6 t^{12}}{3628800}
\end{aligned}$$



In[10]:= SeriesCoefficient[%9, {t, 0, 6}]

Out[10]=

$$\begin{aligned}
& \frac{c_1^6}{3024} - \frac{c_1^4 c_2}{504} + \frac{11 c_1^2 c_2^2}{6048} + \frac{5 c_2^3}{3024} + \frac{5 c_1^3 c_3}{6048} + \frac{11 c_1 c_2 c_3}{6048} - \frac{c_3^2}{6048} - \frac{5 c_1^2 c_4}{6048} - \\
& \frac{c_2 c_4}{672} - \frac{c_1 c_5}{3024} + \frac{c_6}{3024} - \frac{c_1^3 c_2 d_1}{1440} + \frac{1}{480} c_1 c_2^2 d_1 + \frac{c_1^2 c_3 d_1}{1440} - \frac{c_1 c_4 d_1}{1440} - \frac{c_1^4 d_1^2}{1440} + \\
& \frac{1}{360} c_1^2 c_2 d_1^2 + \frac{c_2^2 d_1^2}{480} + \frac{c_1 c_3 d_1^2}{1440} - \frac{c_4 d_1^2}{1440} + \frac{1}{144} c_1 c_2 d_1^3 + \frac{c_1^2 d_1^4}{288} + \frac{c_2 d_1^4}{288} + \\
& \frac{c_1 d_1^5}{240} + \frac{d_1^6}{720} + \frac{c_1^4 d_2}{720} - \frac{1}{180} c_1^2 c_2 d_2 - \frac{c_2^2 d_2}{240} - \frac{c_1 c_3 d_2}{720} + \frac{c_4 d_2}{720} - \frac{1}{48} c_1 c_2 d_1 d_2 - \\
& \frac{1}{72} c_1^2 d_1^2 d_2 - \frac{1}{72} c_2 d_1^2 d_2 - \frac{1}{48} c_1 d_1^3 d_2 - \frac{d_1^4 d_2}{120} + \frac{c_1^2 d_2^2}{144} + \frac{c_2 d_2^2}{144} + \frac{1}{48} c_1 d_1 d_2^2 + \\
& \frac{d_1^2 d_2^2}{80} - \frac{d_2^3}{360} + \frac{c_1 c_2 d_3}{48} + \frac{1}{72} c_1^2 d_1 d_3 + \frac{c_2 d_1 d_3}{72} + \frac{1}{48} c_1 d_1^2 d_3 + \frac{d_1^3 d_3}{120} - \frac{c_1 d_2 d_3}{48} - \\
& \frac{d_1 d_2 d_3}{60} + \frac{d_3^2}{240} - \frac{c_1^2 d_4}{72} - \frac{c_2 d_4}{72} - \frac{c_1 d_1 d_4}{48} - \frac{d_1^2 d_4}{120} + \frac{d_2 d_4}{120} + \frac{c_1 d_5}{48} + \frac{d_1 d_5}{120} - \frac{d_6}{120}
\end{aligned}$$

```
In[11]:= Expand[%10 /. {d1 -> e1 + 10 * t * H, d2 -> e2 + 9 * e1 * t * H + 45 * t^2 * H^2,
d3 -> e3 + 8 * e2 * t * H + 36 * e1 * t^2 * H^2 + 120 * t^3 * H^3,
d4 -> e4 + 7 * e3 * t * H + 28 * e2 * t^2 * H^2 + 84 * e1 * t^3 * H^3 + 210 * t^4 * H^4,
d5 -> e5 + 6 * e4 * t * H + 21 * e3 * t^2 * H^2 + 56 * e2 * t^3 * H^3 +
126 * e1 * t^4 * H^4 + 252 * t^5 * H^5, d6 -> e6 + 5 * e5 * t * H + 15 * e4 * t^2 * H^2 +
35 * e3 * t^3 * H^3 + 70 * e2 * t^4 * H^4 + 126 * e1 * t^5 * H^5 + 210 * t^6 * H^6}]
```

Out[11]=

$$\begin{aligned}
& \frac{c1^6}{3024} - \frac{c1^4 c2}{504} + \frac{11 c1^2 c2^2}{6048} + \frac{5 c2^3}{3024} + \frac{5 c1^3 c3}{6048} + \frac{11 c1 c2 c3}{6048} - \frac{c3^2}{6048} - \frac{5 c1^2 c4}{6048} - \\
& \frac{c2 c4}{672} - \frac{c1 c5}{3024} + \frac{c6}{3024} - \frac{c1^3 c2 e1}{1440} + \frac{1}{480} c1 c2^2 e1 + \frac{c1^2 c3 e1}{1440} - \frac{c1 c4 e1}{1440} - \frac{c1^4 e1^2}{1440} + \\
& \frac{1}{360} c1^2 c2 e1^2 + \frac{c2^2 e1^2}{480} + \frac{c1 c3 e1^2}{1440} - \frac{c4 e1^2}{1440} + \frac{1}{144} c1 c2 e1^3 + \frac{c1^2 e1^4}{288} + \frac{c2 e1^4}{288} + \\
& \frac{c1 e1^5}{240} + \frac{e1^6}{720} + \frac{c1^4 e2}{720} - \frac{1}{180} c1^2 c2 e2 - \frac{c2^2 e2}{240} - \frac{c1 c3 e2}{720} + \frac{c4 e2}{720} - \frac{1}{48} c1 c2 e1 e2 - \\
& \frac{1}{72} c1^2 e1^2 e2 - \frac{1}{72} c2 e1^2 e2 - \frac{1}{48} c1 e1^3 e2 - \frac{e1^4 e2}{120} + \frac{c1^2 e2^2}{144} + \frac{c2 e2^2}{144} + \frac{1}{48} c1 e1 e2^2 + \\
& \frac{e1^2 e2^2}{80} - \frac{e2^3}{360} + \frac{c1 c2 e3}{48} + \frac{1}{72} c1^2 e1 e3 + \frac{c2 e1 e3}{72} + \frac{1}{48} c1 e1^2 e3 + \frac{e1^3 e3}{120} - \frac{c1 e2 e3}{48} - \\
& \frac{e1 e2 e3}{60} + \frac{e3^2}{240} - \frac{c1^2 e4}{72} - \frac{c2 e4}{72} - \frac{c1 e1 e4}{48} - \frac{e1^2 e4}{120} + \frac{e2 e4}{120} + \frac{c1 e5}{48} + \frac{e1 e5}{120} - \frac{e6}{120} - \\
& \frac{1}{144} c1^3 c2 H t + \frac{1}{48} c1 c2^2 H t + \frac{1}{144} c1^2 c3 H t - \frac{1}{144} c1 c4 H t - \frac{1}{720} c1^4 e1 H t + \\
& \frac{1}{180} c1^2 c2 e1 H t + \frac{1}{240} c2^2 e1 H t + \frac{1}{720} c1 c3 e1 H t - \frac{1}{720} c4 e1 H t + \frac{1}{48} c1 c2 e1^2 H t + \\
& \frac{1}{72} c1^2 e1^3 H t + \frac{1}{72} c2 e1^3 H t + \frac{1}{48} c1 e1^4 H t + \frac{1}{120} e1^5 H t - \frac{1}{24} c1 c2 e2 H t - \\
& \frac{1}{24} c1^2 e1 e2 H t - \frac{1}{24} c2 e1 e2 H t - \frac{1}{12} c1 e1^2 e2 H t - \frac{1}{24} e1^3 e2 H t + \frac{1}{24} c1 e2^2 H t + \\
& \frac{1}{24} e1 e2^2 H t + \frac{1}{24} c1^2 e3 H t + \frac{1}{24} c2 e3 H t + \frac{1}{12} c1 e1 e3 H t + \frac{1}{24} e1^2 e3 H t - \\
& \frac{1}{24} e2 e3 H t - \frac{1}{12} c1 e4 H t - \frac{1}{24} e1 e4 H t + \frac{e5 H t}{24} - \frac{1}{144} c1^4 H^2 t^2 + \frac{1}{36} c1^2 c2 H^2 t^2 + \\
& \frac{1}{48} c2^2 H^2 t^2 + \frac{1}{144} c1 c3 H^2 t^2 - \frac{1}{144} c4 H^2 t^2 + \frac{1}{48} c1 c2 e1 H^2 t^2 + \frac{1}{48} c1^2 e1^2 H^2 t^2 + \\
& \frac{1}{48} c2 e1^2 H^2 t^2 + \frac{1}{24} c1 e1^3 H^2 t^2 + \frac{1}{48} e1^4 H^2 t^2 - \frac{1}{24} c1^2 e2 H^2 t^2 - \frac{1}{24} c2 e2 H^2 t^2 - \\
& \frac{1}{8} c1 e1 e2 H^2 t^2 - \frac{1}{12} e1^2 e2 H^2 t^2 + \frac{1}{24} e2^2 H^2 t^2 + \frac{1}{8} c1 e3 H^2 t^2 + \frac{1}{12} e1 e3 H^2 t^2 - \\
& \frac{1}{12} e4 H^2 t^2 + \frac{5}{72} c1 c2 H^3 t^3 + \frac{1}{72} c1^2 e1 H^3 t^3 + \frac{1}{72} c2 e1 H^3 t^3 + \frac{1}{24} c1 e1^2 H^3 t^3 + \\
& \frac{1}{36} e1^3 H^3 t^3 - \frac{1}{12} c1 e2 H^3 t^3 - \frac{1}{12} e1 e2 H^3 t^3 + \frac{1}{12} e3 H^3 t^3 + \frac{5}{144} c1^2 H^4 t^4 + \frac{5}{144} c2 H^4 t^4 + \\
& \frac{1}{48} c1 e1 H^4 t^4 + \frac{1}{48} e1^2 H^4 t^4 - \frac{1}{24} e2 H^4 t^4 + \frac{1}{24} c1 H^5 t^5 + \frac{1}{120} e1 H^5 t^5 + \frac{H^6 t^6}{72}
\end{aligned}$$

In[12]:= **Expand**[(1 + (a + b) \* t) \* (1 + (a + c) \* t) \*  
 (1 + (a + d) \* t) \* (1 + (a + e) \* t) \* (1 + (b + c) \* t) \* (1 + (b + d) \* t) \*  
 (1 + (b + e) \* t) \* (1 + (c + d) \* t) \* (1 + (c + e) \* t) \* (1 + (d + e) \* t)]

Out[12]=

1 + 4 a t + 4 b t + 4 c t + 4 d t + 4 e t + 6 a<sup>2</sup> t<sup>2</sup> + 15 a b t<sup>2</sup> + 6 b<sup>2</sup> t<sup>2</sup> + ... 1605 ... + a c<sup>3</sup> d<sup>2</sup> e<sup>4</sup> t<sup>10</sup> + b c<sup>3</sup> d<sup>2</sup> e<sup>4</sup> t<sup>10</sup> +  
 a<sup>2</sup> b d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + a b<sup>2</sup> d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + a<sup>2</sup> c d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + 2 a b c d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + b<sup>2</sup> c d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + a c<sup>2</sup> d<sup>3</sup> e<sup>4</sup> t<sup>10</sup> + b c<sup>2</sup> d<sup>3</sup> e<sup>4</sup> t<sup>10</sup>

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In[13]:= **G6 = SeriesCoefficient**[%12, {t, 0, 6}]

Out[13]=

3 a<sup>4</sup> b<sup>2</sup> + 7 a<sup>3</sup> b<sup>3</sup> + 3 a<sup>2</sup> b<sup>4</sup> + 8 a<sup>4</sup> b c + 39 a<sup>3</sup> b<sup>2</sup> c + 39 a<sup>2</sup> b<sup>3</sup> c + 8 a b<sup>4</sup> c + 3 a<sup>4</sup> c<sup>2</sup> + 39 a<sup>3</sup> b c<sup>2</sup> +  
 80 a<sup>2</sup> b<sup>2</sup> c<sup>2</sup> + 39 a b<sup>3</sup> c<sup>2</sup> + 3 b<sup>4</sup> c<sup>2</sup> + 7 a<sup>3</sup> c<sup>3</sup> + 39 a<sup>2</sup> b c<sup>3</sup> + 39 a b<sup>2</sup> c<sup>3</sup> + 7 b<sup>3</sup> c<sup>3</sup> + 3 a<sup>2</sup> c<sup>4</sup> +  
 8 a b c<sup>4</sup> + 3 b<sup>2</sup> c<sup>4</sup> + 8 a<sup>4</sup> b d + 39 a<sup>3</sup> b<sup>2</sup> d + 39 a<sup>2</sup> b<sup>3</sup> d + 8 a b<sup>4</sup> d + 8 a<sup>4</sup> c d + 96 a<sup>3</sup> b c d +  
 193 a<sup>2</sup> b<sup>2</sup> c d + 96 a b<sup>3</sup> c d + 8 b<sup>4</sup> c d + 39 a<sup>3</sup> c<sup>2</sup> d + 193 a<sup>2</sup> b c<sup>2</sup> d + 193 a b<sup>2</sup> c<sup>2</sup> d + 39 b<sup>3</sup> c<sup>2</sup> d +  
 39 a<sup>2</sup> c<sup>3</sup> d + 96 a b c<sup>3</sup> d + 39 b<sup>2</sup> c<sup>3</sup> d + 8 a c<sup>4</sup> d + 8 b c<sup>4</sup> d + 3 a<sup>4</sup> d<sup>2</sup> + 39 a<sup>3</sup> b d<sup>2</sup> + 80 a<sup>2</sup> b<sup>2</sup> d<sup>2</sup> +  
 39 a b<sup>3</sup> d<sup>2</sup> + 3 b<sup>4</sup> d<sup>2</sup> + 39 a<sup>3</sup> c d<sup>2</sup> + 193 a<sup>2</sup> b c d<sup>2</sup> + 193 a b<sup>2</sup> c d<sup>2</sup> + 39 b<sup>3</sup> c d<sup>2</sup> + 80 a<sup>2</sup> c<sup>2</sup> d<sup>2</sup> +  
 193 a b c<sup>2</sup> d<sup>2</sup> + 80 b<sup>2</sup> c<sup>2</sup> d<sup>2</sup> + 39 a c<sup>3</sup> d<sup>2</sup> + 39 b c<sup>3</sup> d<sup>2</sup> + 3 c<sup>4</sup> d<sup>2</sup> + 7 a<sup>3</sup> d<sup>3</sup> + 39 a<sup>2</sup> b d<sup>3</sup> +  
 39 a b<sup>2</sup> d<sup>3</sup> + 7 b<sup>3</sup> d<sup>3</sup> + 39 a<sup>2</sup> c d<sup>3</sup> + 96 a b c d<sup>3</sup> + 39 b<sup>2</sup> c d<sup>3</sup> + 39 a c<sup>2</sup> d<sup>3</sup> + 39 b c<sup>2</sup> d<sup>3</sup> + 7 c<sup>3</sup> d<sup>3</sup> +  
 3 a<sup>2</sup> d<sup>4</sup> + 8 a b d<sup>4</sup> + 3 b<sup>2</sup> d<sup>4</sup> + 8 a c d<sup>4</sup> + 8 b c d<sup>4</sup> + 3 c<sup>2</sup> d<sup>4</sup> + 8 a<sup>4</sup> b e + 39 a<sup>3</sup> b<sup>2</sup> e + 39 a<sup>2</sup> b<sup>3</sup> e +  
 8 a b<sup>4</sup> e + 8 a<sup>4</sup> c e + 96 a<sup>3</sup> b c e + 193 a<sup>2</sup> b<sup>2</sup> c e + 96 a b<sup>3</sup> c e + 8 b<sup>4</sup> c e + 39 a<sup>3</sup> c<sup>2</sup> e +  
 193 a<sup>2</sup> b c<sup>2</sup> e + 193 a b<sup>2</sup> c<sup>2</sup> e + 39 b<sup>3</sup> c<sup>2</sup> e + 39 a<sup>2</sup> c<sup>3</sup> e + 96 a b c<sup>3</sup> e + 39 b<sup>2</sup> c<sup>3</sup> e + 8 a c<sup>4</sup> e +  
 8 b c<sup>4</sup> e + 8 a<sup>4</sup> d e + 96 a<sup>3</sup> b d e + 193 a<sup>2</sup> b<sup>2</sup> d e + 96 a b<sup>3</sup> d e + 8 b<sup>4</sup> d e + 96 a<sup>3</sup> c d e +  
 444 a<sup>2</sup> b c d e + 444 a b<sup>2</sup> c d e + 96 b<sup>3</sup> c d e + 193 a<sup>2</sup> c<sup>2</sup> d e + 444 a b c<sup>2</sup> d e + 193 b<sup>2</sup> c<sup>2</sup> d e +  
 96 a c<sup>3</sup> d e + 96 b c<sup>3</sup> d e + 8 c<sup>4</sup> d e + 39 a<sup>3</sup> d<sup>2</sup> e + 193 a<sup>2</sup> b d<sup>2</sup> e + 193 a b<sup>2</sup> d<sup>2</sup> e + 39 b<sup>3</sup> d<sup>2</sup> e +  
 193 a<sup>2</sup> c d<sup>2</sup> e + 444 a b c d<sup>2</sup> e + 193 b<sup>2</sup> c d<sup>2</sup> e + 193 a c<sup>2</sup> d<sup>2</sup> e + 193 b c<sup>2</sup> d<sup>2</sup> e + 39 c<sup>3</sup> d<sup>2</sup> e +  
 39 a<sup>2</sup> d<sup>3</sup> e + 96 a b d<sup>3</sup> e + 39 b<sup>2</sup> d<sup>3</sup> e + 96 a c d<sup>3</sup> e + 96 b c d<sup>3</sup> e + 39 c<sup>2</sup> d<sup>3</sup> e + 8 a d<sup>4</sup> e +  
 8 b d<sup>4</sup> e + 8 c d<sup>4</sup> e + 3 a<sup>4</sup> e<sup>2</sup> + 39 a<sup>3</sup> b e<sup>2</sup> + 80 a<sup>2</sup> b<sup>2</sup> e<sup>2</sup> + 39 a b<sup>3</sup> e<sup>2</sup> + 3 b<sup>4</sup> e<sup>2</sup> + 39 a<sup>3</sup> c e<sup>2</sup> +  
 193 a<sup>2</sup> b c e<sup>2</sup> + 193 a b<sup>2</sup> c e<sup>2</sup> + 39 b<sup>3</sup> c e<sup>2</sup> + 80 a<sup>2</sup> c<sup>2</sup> e<sup>2</sup> + 193 a b c<sup>2</sup> e<sup>2</sup> + 80 b<sup>2</sup> c<sup>2</sup> e<sup>2</sup> + 39 a c<sup>3</sup> e<sup>2</sup> +  
 39 b c<sup>3</sup> e<sup>2</sup> + 3 c<sup>4</sup> e<sup>2</sup> + 39 a<sup>3</sup> d e<sup>2</sup> + 193 a<sup>2</sup> b d e<sup>2</sup> + 193 a b<sup>2</sup> d e<sup>2</sup> + 39 b<sup>3</sup> d e<sup>2</sup> + 193 a<sup>2</sup> c d e<sup>2</sup> +  
 444 a b c d e<sup>2</sup> + 193 b<sup>2</sup> c d e<sup>2</sup> + 193 a c<sup>2</sup> d e<sup>2</sup> + 193 b c<sup>2</sup> d e<sup>2</sup> + 39 c<sup>3</sup> d e<sup>2</sup> + 80 a<sup>2</sup> d<sup>2</sup> e<sup>2</sup> +  
 193 a b d<sup>2</sup> e<sup>2</sup> + 80 b<sup>2</sup> d<sup>2</sup> e<sup>2</sup> + 193 a c d<sup>2</sup> e<sup>2</sup> + 193 b c d<sup>2</sup> e<sup>2</sup> + 80 c<sup>2</sup> d<sup>2</sup> e<sup>2</sup> + 39 a d<sup>3</sup> e<sup>2</sup> +  
 39 b d<sup>3</sup> e<sup>2</sup> + 39 c d<sup>3</sup> e<sup>2</sup> + 3 d<sup>4</sup> e<sup>2</sup> + 7 a<sup>3</sup> e<sup>3</sup> + 39 a<sup>2</sup> b e<sup>3</sup> + 39 a b<sup>2</sup> e<sup>3</sup> + 7 b<sup>3</sup> e<sup>3</sup> + 39 a<sup>2</sup> c e<sup>3</sup> +  
 96 a b c e<sup>3</sup> + 39 b<sup>2</sup> c e<sup>3</sup> + 39 a c<sup>2</sup> e<sup>3</sup> + 39 b c<sup>2</sup> e<sup>3</sup> + 7 c<sup>3</sup> e<sup>3</sup> + 39 a<sup>2</sup> d e<sup>3</sup> + 96 a b d e<sup>3</sup> + 39 b<sup>2</sup> d e<sup>3</sup> +  
 96 a c d e<sup>3</sup> + 96 b c d e<sup>3</sup> + 39 c<sup>2</sup> d e<sup>3</sup> + 39 a d<sup>2</sup> e<sup>3</sup> + 39 b d<sup>2</sup> e<sup>3</sup> + 39 c d<sup>2</sup> e<sup>3</sup> + 7 d<sup>3</sup> e<sup>3</sup> + 3 a<sup>2</sup> e<sup>4</sup> +  
 8 a b e<sup>4</sup> + 3 b<sup>2</sup> e<sup>4</sup> + 8 a c e<sup>4</sup> + 8 b c e<sup>4</sup> + 3 c<sup>2</sup> e<sup>4</sup> + 8 a d e<sup>4</sup> + 8 b d e<sup>4</sup> + 8 c d e<sup>4</sup> + 3 d<sup>2</sup> e<sup>4</sup>

In[14]:= **G5 = SeriesCoefficient[%12, {t, 0, 5}]**

Out[14]=

$$\begin{aligned}
& 3 a^4 b + 15 a^3 b^2 + 15 a^2 b^3 + 3 a b^4 + 3 a^4 c + 38 a^3 b c + 78 a^2 b^2 c + 38 a b^3 c + 3 b^4 c + \\
& 15 a^3 c^2 + 78 a^2 b c^2 + 78 a b^2 c^2 + 15 b^3 c^2 + 15 a^2 c^3 + 38 a b c^3 + 15 b^2 c^3 + 3 a c^4 + \\
& 3 b c^4 + 3 a^4 d + 38 a^3 b d + 78 a^2 b^2 d + 38 a b^3 d + 3 b^4 d + 38 a^3 c d + 189 a^2 b c d + \\
& 189 a b^2 c d + 38 b^3 c d + 78 a^2 c^2 d + 189 a b c^2 d + 78 b^2 c^2 d + 38 a c^3 d + 38 b c^3 d + \\
& 3 c^4 d + 15 a^3 d^2 + 78 a^2 b d^2 + 78 a b^2 d^2 + 15 b^3 d^2 + 78 a^2 c d^2 + 189 a b c d^2 + \\
& 78 b^2 c d^2 + 78 a c^2 d^2 + 78 b c^2 d^2 + 15 c^3 d^2 + 15 a^2 d^3 + 38 a b d^3 + 15 b^2 d^3 + 38 a c d^3 + \\
& 38 b c d^3 + 15 c^2 d^3 + 3 a d^4 + 3 b d^4 + 3 c d^4 + 3 a^4 e + 38 a^3 b e + 78 a^2 b^2 e + 38 a b^3 e + \\
& 3 b^4 e + 38 a^3 c e + 189 a^2 b c e + 189 a b^2 c e + 38 b^3 c e + 78 a^2 c^2 e + 189 a b c^2 e + \\
& 78 b^2 c^2 e + 38 a c^3 e + 38 b c^3 e + 3 c^4 e + 38 a^3 d e + 189 a^2 b d e + 189 a b^2 d e + \\
& 38 b^3 d e + 189 a^2 c d e + 444 a b c d e + 189 b^2 c d e + 189 a c^2 d e + 189 b c^2 d e + \\
& 38 c^3 d e + 78 a^2 d^2 e + 189 a b d^2 e + 78 b^2 d^2 e + 189 a c d^2 e + 189 b c d^2 e + 78 c^2 d^2 e + \\
& 38 a d^3 e + 38 b d^3 e + 38 c d^3 e + 3 d^4 e + 15 a^3 e^2 + 78 a^2 b e^2 + 78 a b^2 e^2 + 15 b^3 e^2 + \\
& 78 a^2 c e^2 + 189 a b c e^2 + 78 b^2 c e^2 + 78 a c^2 e^2 + 78 b c^2 e^2 + 15 c^3 e^2 + 78 a^2 d e^2 + \\
& 189 a b d e^2 + 78 b^2 d e^2 + 189 a c d e^2 + 189 b c d e^2 + 78 c^2 d e^2 + 78 a d^2 e^2 + \\
& 78 b d^2 e^2 + 78 c d^2 e^2 + 15 d^3 e^2 + 15 a^2 e^3 + 38 a b e^3 + 15 b^2 e^3 + 38 a c e^3 + 38 b c e^3 + \\
& 15 c^2 e^3 + 38 a d e^3 + 38 b d e^3 + 38 c d e^3 + 15 d^2 e^3 + 3 a e^4 + 3 b e^4 + 3 c e^4 + 3 d e^4
\end{aligned}$$

In[15]:= **G4 = SeriesCoefficient[%12, {t, 0, 4}]**

Out[15]=

$$\begin{aligned}
& a^4 + 13 a^3 b + 27 a^2 b^2 + 13 a b^3 + b^4 + 13 a^3 c + 67 a^2 b c + 67 a b^2 c + 13 b^3 c + 27 a^2 c^2 + \\
& 67 a b c^2 + 27 b^2 c^2 + 13 a c^3 + 13 b c^3 + c^4 + 13 a^3 d + 67 a^2 b d + 67 a b^2 d + 13 b^3 d + \\
& 67 a^2 c d + 163 a b c d + 67 b^2 c d + 67 a c^2 d + 67 b c^2 d + 13 c^3 d + 27 a^2 d^2 + 67 a b d^2 + \\
& 27 b^2 d^2 + 67 a c d^2 + 67 b c d^2 + 27 c^2 d^2 + 13 a d^3 + 13 b d^3 + 13 c d^3 + d^4 + 13 a^3 e + \\
& 67 a^2 b e + 67 a b^2 e + 13 b^3 e + 67 a^2 c e + 163 a b c e + 67 b^2 c e + 67 a c^2 e + 67 b c^2 e + \\
& 13 c^3 e + 67 a^2 d e + 163 a b d e + 67 b^2 d e + 163 a c d e + 163 b c d e + 67 c^2 d e + 67 a d^2 e + \\
& 67 b d^2 e + 67 c d^2 e + 13 d^3 e + 27 a^2 e^2 + 67 a b e^2 + 27 b^2 e^2 + 67 a c e^2 + 67 b c e^2 + \\
& 27 c^2 e^2 + 67 a d e^2 + 67 b d e^2 + 67 c d e^2 + 27 d^2 e^2 + 13 a e^3 + 13 b e^3 + 13 c e^3 + 13 d e^3 + e^4
\end{aligned}$$

In[16]:= **G3 = SeriesCoefficient[%12, {t, 0, 3}]**

Out[16]=

$$\begin{aligned}
& 4 a^3 + 21 a^2 b + 21 a b^2 + 4 b^3 + 21 a^2 c + 52 a b c + 21 b^2 c + 21 a c^2 + 21 b c^2 + \\
& 4 c^3 + 21 a^2 d + 52 a b d + 21 b^2 d + 52 a c d + 52 b c d + 21 c^2 d + 21 a d^2 + \\
& 21 b d^2 + 21 c d^2 + 4 d^3 + 21 a^2 e + 52 a b e + 21 b^2 e + 52 a c e + 52 b c e + 21 c^2 e + \\
& 52 a d e + 52 b d e + 52 c d e + 21 d^2 e + 21 a e^2 + 21 b e^2 + 21 c e^2 + 21 d e^2 + 4 e^3
\end{aligned}$$

In[17]:= **G2 = SeriesCoefficient[%12, {t, 0, 2}]**

Out[17]=

$$\begin{aligned}
& 6 a^2 + 15 a b + 6 b^2 + 15 a c + 15 b c + 6 c^2 + 15 a d + \\
& 15 b d + 15 c d + 6 d^2 + 15 a e + 15 b e + 15 c e + 15 d e + 6 e^2
\end{aligned}$$

In[18]:= **G1 = SeriesCoefficient[%12, {t, 0, 1}]**

Out[18]=

$$4 (a + b + c + d + e)$$

In[19]:= **SymmetricReduction[G6, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[19]=

$$\{3 f_1^2 f_2^2 + f_2^3 + 2 f_1^3 f_3 + 6 f_1 f_2 f_3 - f_3^2 - 2 f_1^2 f_4 - 2 f_2 f_4 - 22 f_1 f_5, 0\}$$

In[20]:= **k6 = First[%19]**

Out[20]=  
 $3 f_1^2 f_2^2 + f_2^3 + 2 f_1^3 f_3 + 6 f_1 f_2 f_3 - f_3^2 - 2 f_1^2 f_4 - 2 f_2 f_4 - 22 f_1 f_5$

In[21]:= **SymmetricReduction[G5, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[21]=  
 $\{3 f_1^3 f_2 + 6 f_1 f_2^2 + 5 f_1^2 f_3 + 2 f_2 f_3 - 5 f_1 f_4 - 11 f_5, 0\}$

In[22]:= **k5 = First[%21]**

Out[22]=  
 $3 f_1^3 f_2 + 6 f_1 f_2^2 + 5 f_1^2 f_3 + 2 f_2 f_3 - 5 f_1 f_4 - 11 f_5$

In[23]:= **SymmetricReduction[G4, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[23]=  
 $\{f_1^4 + 9 f_1^2 f_2 + 3 f_2^2 + 4 f_1 f_3 - 3 f_4, 0\}$

In[24]:= **k4 = First[%23]**

Out[24]=  
 $f_1^4 + 9 f_1^2 f_2 + 3 f_2^2 + 4 f_1 f_3 - 3 f_4$

In[25]:= **SymmetricReduction[G3, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[25]=  
 $\{4 f_1^3 + 9 f_1 f_2 + f_3, 0\}$

In[26]:= **k3 = First[%25]**

Out[26]=  
 $4 f_1^3 + 9 f_1 f_2 + f_3$

In[27]:= **SymmetricReduction[G2, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[27]=  
 $\{6 f_1^2 + 3 f_2, 0\}$

In[28]:= **k2 = First[%27]**

Out[28]=  
 $6 f_1^2 + 3 f_2$

In[29]:= **SymmetricReduction[G1, {a, b, c, d, e}, {f1, f2, f3, f4, f5}]**

Out[29]=  
 $\{4 f_1, 0\}$

In[30]:= **k1 = First[%29]**

Out[30]=  
 $4 f_1$

In[31]:= `p1 = Expand[%11 /. {e1 -> k1, e2 -> k2, e3 -> k3, e4 -> k4, e5 -> k5, e6 -> k6}]`

Out[31]=

$$\begin{aligned}
& \frac{c1^6}{3024} - \frac{c1^4 c2}{504} + \frac{11 c1^2 c2^2}{6048} + \frac{5 c2^3}{3024} + \frac{5 c1^3 c3}{6048} + \frac{11 c1 c2 c3}{6048} - \frac{c3^2}{6048} - \frac{5 c1^2 c4}{6048} - \frac{c2 c4}{672} - \\
& \frac{c1 c5}{3024} + \frac{c6}{3024} - \frac{1}{360} c1^3 c2 f1 + \frac{1}{120} c1 c2^2 f1 + \frac{1}{360} c1^2 c3 f1 - \frac{c1 c4 f1}{360} - \frac{c1^4 f1^2}{360} + \\
& \frac{1}{90} c1^2 c2 f1^2 + \frac{c2^2 f1^2}{120} + \frac{1}{360} c1 c3 f1^2 - \frac{c4 f1^2}{360} + \frac{1}{36} c1 c2 f1^3 + \frac{c1^2 f1^4}{72} + \frac{c2 f1^4}{72} + \\
& \frac{c1 f1^5}{60} + \frac{f1^6}{180} + \frac{c1^4 f2}{240} - \frac{1}{60} c1^2 c2 f2 - \frac{c2^2 f2}{80} - \frac{c1 c3 f2}{240} + \frac{c4 f2}{240} - \frac{1}{16} c1 c2 f1 f2 - \\
& \frac{1}{24} c1^2 f1^2 f2 - \frac{1}{24} c2 f1^2 f2 - \frac{1}{16} c1 f1^3 f2 - \frac{f1^4 f2}{40} + \frac{c1^2 f2^2}{48} + \frac{c2 f2^2}{48} + \frac{1}{16} c1 f1 f2^2 + \\
& \frac{3 f1^2 f2^2}{80} - \frac{f2^3}{120} + \frac{c1 c2 f3}{48} - \frac{1}{48} c1 f1^2 f3 - \frac{f1^3 f3}{60} - \frac{c1 f2 f3}{48} - \frac{f1 f2 f3}{120} + \frac{f3^2}{80} + \\
& \frac{c1^2 f4}{24} + \frac{c2 f4}{24} + \frac{7 c1 f1 f4}{48} + \frac{f1^2 f4}{10} - \frac{7 f2 f4}{120} - \frac{11 c1 f5}{48} - \frac{11 f1 f5}{60} - \frac{1}{144} c1^3 c2 H t + \\
& \frac{1}{48} c1 c2^2 H t + \frac{1}{144} c1^2 c3 H t - \frac{1}{144} c1 c4 H t - \frac{1}{180} c1^4 f1 H t + \frac{1}{45} c1^2 c2 f1 H t + \\
& \frac{1}{60} c2^2 f1 H t + \frac{1}{180} c1 c3 f1 H t - \frac{1}{180} c4 f1 H t + \frac{1}{12} c1 c2 f1^2 H t + \frac{1}{18} c1^2 f1^3 H t + \\
& \frac{1}{18} c2 f1^3 H t + \frac{1}{12} c1 f1^4 H t + \frac{1}{30} f1^5 H t - \frac{1}{8} c1 c2 f2 H t - \frac{1}{8} c1^2 f1 f2 H t - \\
& \frac{1}{8} c2 f1 f2 H t - \frac{1}{4} c1 f1^2 f2 H t - \frac{1}{8} f1^3 f2 H t + \frac{1}{8} c1 f2^2 H t + \frac{1}{8} f1 f2^2 H t + \frac{1}{24} c1^2 f3 H t + \\
& \frac{1}{24} c2 f3 H t - \frac{1}{24} f1^2 f3 H t - \frac{1}{24} f2 f3 H t + \frac{1}{4} c1 f4 H t + \frac{7}{24} f1 f4 H t - \frac{11 f5 H t}{24} - \\
& \frac{1}{144} c1^4 H^2 t^2 + \frac{1}{36} c1^2 c2 H^2 t^2 + \frac{1}{48} c2^2 H^2 t^2 + \frac{1}{144} c1 c3 H^2 t^2 - \frac{1}{144} c4 H^2 t^2 + \\
& \frac{1}{12} c1 c2 f1 H^2 t^2 + \frac{1}{12} c1^2 f1^2 H^2 t^2 + \frac{1}{12} c2 f1^2 H^2 t^2 + \frac{1}{6} c1 f1^3 H^2 t^2 + \frac{1}{12} f1^4 H^2 t^2 - \\
& \frac{1}{8} c1^2 f2 H^2 t^2 - \frac{1}{8} c2 f2 H^2 t^2 - \frac{3}{8} c1 f1 f2 H^2 t^2 - \frac{1}{4} f1^2 f2 H^2 t^2 + \frac{1}{8} f2^2 H^2 t^2 + \\
& \frac{1}{8} c1 f3 H^2 t^2 + \frac{1}{4} f4 H^2 t^2 + \frac{5}{72} c1 c2 H^3 t^3 + \frac{1}{18} c1^2 f1 H^3 t^3 + \frac{1}{18} c2 f1 H^3 t^3 + \\
& \frac{1}{6} c1 f1^2 H^3 t^3 + \frac{1}{9} f1^3 H^3 t^3 - \frac{1}{4} c1 f2 H^3 t^3 - \frac{1}{4} f1 f2 H^3 t^3 + \frac{1}{12} f3 H^3 t^3 + \frac{5}{144} c1^2 H^4 t^4 + \\
& \frac{5}{144} c2 H^4 t^4 + \frac{1}{12} c1 f1 H^4 t^4 + \frac{1}{12} f1^2 H^4 t^4 - \frac{1}{8} f2 H^4 t^4 + \frac{1}{24} c1 H^5 t^5 + \frac{1}{30} f1 H^5 t^5 + \frac{H^6 t^6}{72}
\end{aligned}$$

In[32]:= `FunctionExpand[1 - Binomial[5 - d, 5]]`

Out[32]=

$$1 - \frac{1}{120} (1 - d) (2 - d) (3 - d) (4 - d) (5 - d)$$

In[33]:= **Expand**[(1/4) \* l1 \* l2 \* f1 +  
 (1/4) \* (l1^2 + l2) \* (f1^2 - 2 \* f2) + (1/2) \* l1 \* (f1^3 - 3 \* f1 \* f2 + 3 \* f3) +  
 (1/4) \* (f1^4 - 4 \* f1^2 \* f2 + 4 \* f1 \* f3 + 2 \* f2^2) - 30 \* d + 30 \* %32]

Out[33]=  

$$\frac{77 d}{2} - \frac{225 d^2}{4} + \frac{85 d^3}{4} - \frac{15 d^4}{4} + \frac{d^5}{4} + \frac{f1^4}{4} - f1^2 f2 + \frac{f2^2}{2} + f1 f3 +$$

$$\frac{f1^3 l1}{2} - \frac{3 f1 f2 l1}{2} + \frac{3 f3 l1}{2} + \frac{f1^2 l1^2}{4} - \frac{f2 l1^2}{2} + \frac{f1^2 l2}{4} - \frac{f2 l2}{2} + \frac{f1 l1 l2}{4}$$

In[34]:= **Expand**[%33 /. {l1 -> (6 - d) \* H, l2 -> (d^2 - 6 \* d + 15) \* H^2, f1 -> (5/2) \* (d - 1) \* H,  
 f2 -> (5/24) \* (d - 1) \* (13 \* d - 11) \* H^2, f3 -> (5/16) \* (d - 1)^2 \* (5 \* d - 3) \* H^3}]

Out[34]=  

$$\frac{77 d}{2} - \frac{225 d^2}{4} + \frac{85 d^3}{4} - \frac{15 d^4}{4} + \frac{d^5}{4} -$$

$$\frac{44 165 H^4}{1152} + \frac{885 d H^4}{16} - \frac{11 155 d^2 H^4}{576} + \frac{35 d^3 H^4}{16} + \frac{235 d^4 H^4}{1152}$$

In[35]:= **Expand**[%34 /. {H^4 -> d}]

Out[35]=  

$$\frac{187 d}{1152} - \frac{15 d^2}{16} + \frac{1085 d^3}{576} - \frac{25 d^4}{16} + \frac{523 d^5}{1152}$$

In[36]:= **Expand**[(1/d) \* %35]

Out[36]=  

$$\frac{187}{1152} - \frac{15 d}{16} + \frac{1085 d^2}{576} - \frac{25 d^3}{16} + \frac{523 d^4}{1152}$$

In[37]:= **Factor**[%36]

Out[37]=  

$$\frac{(-1 + d) (-187 + 893 d - 1277 d^2 + 523 d^3)}{1152}$$

In[38]:= **FunctionExpand**[1 - Binomial[6 - d, 6]]

Out[38]=  

$$1 - \frac{1}{720} (-6 + d) (-5 + d) (-4 + d) (-3 + d) (-2 + d) (-1 + d)$$

In[39]:= **Expand**[ $24 * 5 * (H^5 - \%38) - (1/5) * (f1^5) + (f1^3) * (f2) - (f1^2) * (f3) -$   
 $(f1) * (f2^2) + (f1) * (f4) + (f2) * (f3) + (1/2) * (f1^2 - 2 * f2) * l2 * (d - 7) * H +$   
 $(1/30) * f1 * ((d - 7)^4 * H^4 - 4 * (d - 7)^2 * H^2 * l2 + (d - 7) * H * l3 - 3 * l2^2 + l4) +$   
 $(1/2) * (f1^4 - 4 * f1^2 * f2 + 4 * f1 * f3 + 2 * f2^2 - 4 * f4) * (d - 7) * H -$   
 $(1/3) * ((d - 7)^2 * H^2 + l2) * (f1^3 - 3 * f1 * f2 + 3 * f3) ]$

Out[39]=

$$-294 d + \frac{812 d^2}{3} - \frac{245 d^3}{2} + \frac{175 d^4}{6} - \frac{7 d^5}{2} + \frac{d^6}{6} - \frac{f1^5}{5} + f1^3 f2 - f1 f2^2 - f1^2 f3 +$$

$$f2 f3 + f1 f4 - \frac{7 f1^4 H}{2} + \frac{1}{2} d f1^4 H + 14 f1^2 f2 H - 2 d f1^2 f2 H - 7 f2^2 H + d f2^2 H -$$

$$14 f1 f3 H + 2 d f1 f3 H + 14 f4 H - 2 d f4 H - \frac{49 f1^3 H^2}{3} + \frac{14}{3} d f1^3 H^2 - \frac{1}{3} d^2 f1^3 H^2 +$$

$$49 f1 f2 H^2 - 14 d f1 f2 H^2 + d^2 f1 f2 H^2 - 49 f3 H^2 + 14 d f3 H^2 - d^2 f3 H^2 +$$

$$\frac{2401 f1 H^4}{30} - \frac{686}{15} d f1 H^4 + \frac{49}{5} d^2 f1 H^4 - \frac{14}{15} d^3 f1 H^4 + \frac{1}{30} d^4 f1 H^4 + 120 H^5 - \frac{f1^3 l2}{3} +$$

$$f1 f2 l2 - f3 l2 - \frac{7}{2} f1^2 H l2 + \frac{1}{2} d f1^2 H l2 + 7 f2 H l2 - d f2 H l2 - \frac{98}{15} f1 H^2 l2 +$$

$$\frac{28}{15} d f1 H^2 l2 - \frac{2}{15} d^2 f1 H^2 l2 - \frac{f1 l2^2}{10} - \frac{7 f1 H l3}{30} + \frac{1}{30} d f1 H l3 + \frac{f1 l4}{30}$$

In[40]:= **Expand**[ $\%39 /. \{l2 \rightarrow (d^2 - 7 * d + 21) * H^2, l3 \rightarrow (35 - 21 * d + 7 * d^2 - d^3) * H^3,$   
 $l4 \rightarrow (d^4 - 7 * d^3 + 21 * d^2 - 35 * d + 35) * H^4,$   
 $f1 \rightarrow (5/2) * (d - 1) * H, f2 \rightarrow (5/24) * (d - 1) * (13 * d - 11) * H^2,$   
 $f3 \rightarrow (5/16) * (d - 1)^2 * (5 * d - 3) * H^3, f4 \rightarrow \%37 * H^4\}$ ]

Out[40]=

$$-294 d + \frac{812 d^2}{3} - \frac{245 d^3}{2} + \frac{175 d^4}{6} - \frac{7 d^5}{2} + \frac{d^6}{6} + \frac{677357 H^5}{2304} -$$

$$\frac{623429 d H^5}{2304} + \frac{140815 d^2 H^5}{1152} - \frac{33175 d^3 H^5}{1152} + \frac{7541 d^4 H^5}{2304} - \frac{269 d^5 H^5}{2304}$$

In[41]:= **Expand**[ $\%40 /. \{H^5 \rightarrow d\}$ ]

Out[41]=

$$-\frac{19 d}{2304} + \frac{187 d^2}{2304} - \frac{305 d^3}{1152} + \frac{425 d^4}{1152} - \frac{523 d^5}{2304} + \frac{115 d^6}{2304}$$

In[42]:= **Expand**[ $(1/d) * \%41$ ]

Out[42]=

$$-\frac{19}{2304} + \frac{187 d}{2304} - \frac{305 d^2}{1152} + \frac{425 d^3}{1152} - \frac{523 d^4}{2304} + \frac{115 d^5}{2304}$$

In[43]:= **Factor**[ $\%42$ ]

Out[43]=

$$\frac{(-1 + d)^2 (-1 + 5 d) (19 - 54 d + 23 d^2)}{2304}$$



In[44]:= Expand[p1 /.

{c1 → (8 - d) \* H, c2 → (d^2 - 8 \* d + 28) \* H^2, c3 → (56 - 28 \* d + 8 \* d^2 - d^3) \* H^3,  
 c4 → (d^4 - 8 \* d^3 + 28 \* d^2 - 56 \* d + 70) \* H^4,  
 c5 → (56 - 70 \* d + 56 \* d^2 - 28 \* d^3 + 8 \* d^4 - d^5) \* H^5,  
 c6 → (d^6 - 8 \* d^5 + 28 \* d^4 - 56 \* d^3 + 70 \* d^2 - 56 \* d + 28) \* H^6,  
 f1 → (5 / 2) \* (d - 1) \* H, f2 → (5 / 24) \* (d - 1) \* (13 \* d - 11) \* H^2,  
 f3 → (5 / 16) \* (d - 1)^2 \* (5 \* d - 3) \* H^3, f4 → %37 \* H^4, f5 → %43 \* H^5}]

Out[44]=

$$\frac{4172519 H^6}{1548288} + \frac{443 d H^6}{96} + \frac{175303 d^2 H^6}{73728} + \frac{5 d^3 H^6}{12} - \frac{5167 d^4 H^6}{73728} - \frac{d^5 H^6}{32} - \frac{3935 d^6 H^6}{1548288} +$$

$$\frac{443 H^6 t}{48} + \frac{3161}{288} d H^6 t + \frac{125}{32} d^2 H^6 t + \frac{65}{144} d^3 H^6 t - \frac{5}{96} d^4 H^6 t - \frac{1}{96} d^5 H^6 t + \frac{3161 H^6 t^2}{288} +$$

$$\frac{295}{32} d H^6 t^2 + \frac{425}{192} d^2 H^6 t^2 + \frac{5}{32} d^3 H^6 t^2 - \frac{5}{576} d^4 H^6 t^2 + \frac{295 H^6 t^3}{48} + \frac{1015}{288} d H^6 t^3 +$$

$$\frac{25}{48} d^2 H^6 t^3 + \frac{5}{288} d^3 H^6 t^3 + \frac{1015 H^6 t^4}{576} + \frac{5}{8} d H^6 t^4 + \frac{25}{576} d^2 H^6 t^4 + \frac{H^6 t^5}{4} + \frac{1}{24} d H^6 t^5 + \frac{H^6 t^6}{72}$$

In[45]:= Expand[%44 /. {H^6 → d}]

Out[45]=

$$\frac{4172519 d}{1548288} + \frac{443 d^2}{96} + \frac{175303 d^3}{73728} + \frac{5 d^4}{12} - \frac{5167 d^5}{73728} - \frac{d^6}{32} - \frac{3935 d^7}{1548288} +$$

$$\frac{443 d t}{48} + \frac{3161 d^2 t}{288} + \frac{125 d^3 t}{32} + \frac{65 d^4 t}{144} - \frac{5 d^5 t}{96} - \frac{d^6 t}{96} + \frac{3161 d t^2}{288} +$$

$$\frac{295 d^2 t^2}{32} + \frac{425 d^3 t^2}{192} + \frac{5 d^4 t^2}{32} - \frac{5 d^5 t^2}{576} + \frac{295 d t^3}{48} + \frac{1015 d^2 t^3}{288} +$$

$$\frac{25 d^3 t^3}{48} + \frac{5 d^4 t^3}{288} + \frac{1015 d t^4}{576} + \frac{5 d^2 t^4}{8} + \frac{25 d^3 t^4}{576} + \frac{d t^5}{4} + \frac{d^2 t^5}{24} + \frac{d t^6}{72}$$

In[46]:= Expand[p1 /.

{c1 → (8 - d) \* H, c2 → (d^2 - 8 \* d + 28) \* H^2, c3 → (56 - 28 \* d + 8 \* d^2 - d^3) \* H^3,  
 c4 → (d^4 - 8 \* d^3 + 28 \* d^2 - 56 \* d + 70) \* H^4,  
 c5 → (56 - 70 \* d + 56 \* d^2 - 28 \* d^3 + 8 \* d^4 - d^5) \* H^5,  
 c6 → (d^6 - 8 \* d^5 + 28 \* d^4 - 56 \* d^3 + 70 \* d^2 - 56 \* d + 28) \* H^6,  
 f1 → -(5 / 2) \* (d - 1) \* H, f2 → (5 / 24) \* (d - 1) \* (13 \* d - 11) \* H^2,  
 f3 → -(5 / 16) \* (d - 1)^2 \* (5 \* d - 3) \* H^3, f4 → %37 \* H^4, f5 → %43 \* (-1) \* H^5}]

Out[46]=

$$\frac{234265319 H^6}{1548288} - \frac{9885 d H^6}{32} + \frac{18495175 d^2 H^6}{73728} - \frac{4975 d^3 H^6}{48} + \frac{1676753 d^4 H^6}{73728} -$$

$$\frac{235 d^5 H^6}{96} + \frac{146593 d^6 H^6}{1548288} + \frac{3295 H^6 t}{16} - \frac{32681}{96} d H^6 t + \frac{61975}{288} d^2 H^6 t - 65 d^3 H^6 t +$$

$$\frac{2675}{288} d^4 H^6 t - \frac{47}{96} d^5 H^6 t + \frac{32681 H^6 t^2}{288} - \frac{4675}{32} d H^6 t^2 + \frac{12965}{192} d^2 H^6 t^2 -$$

$$\frac{425}{32} d^3 H^6 t^2 + \frac{535}{576} d^4 H^6 t^2 + \frac{4675 H^6 t^3}{144} - \frac{2935}{96} d H^6 t^3 + \frac{1325}{144} d^2 H^6 t^3 -$$

$$\frac{85}{96} d^3 H^6 t^3 + \frac{2935 H^6 t^4}{576} - \frac{25}{8} d H^6 t^4 + \frac{265}{576} d^2 H^6 t^4 + \frac{5 H^6 t^5}{12} - \frac{1}{8} d H^6 t^5 + \frac{H^6 t^6}{72}$$

In[47]:= **Expand[%46 /. {t → t + (5/2) \* (d - 1)}]**

Out[47]=

$$\begin{aligned} & \frac{245\,519\,H^6}{1\,548\,288} + \frac{395\,d\,H^6}{192} + \frac{32\,695\,d^2\,H^6}{8192} + \frac{275\,d^3\,H^6}{96} + \frac{62\,953\,d^4\,H^6}{73\,728} + \\ & \frac{5\,d^5\,H^6}{64} - \frac{5447\,d^6\,H^6}{1\,548\,288} + \frac{395\,H^6\,t}{192} + \frac{1181}{144}\,d\,H^6\,t + \frac{2675}{288}\,d^2\,H^6\,t + \frac{1205}{288}\,d^3\,H^6\,t + \\ & \frac{425}{576}\,d^4\,H^6\,t + \frac{1}{32}\,d^5\,H^6\,t + \frac{1181\,H^6\,t^2}{288} + \frac{925}{96}\,d\,H^6\,t^2 + \frac{1315}{192}\,d^2\,H^6\,t^2 + \\ & \frac{175}{96}\,d^3\,H^6\,t^2 + \frac{85}{576}\,d^4\,H^6\,t^2 + \frac{925\,H^6\,t^3}{288} + \frac{685}{144}\,d\,H^6\,t^3 + \frac{575}{288}\,d^2\,H^6\,t^3 + \\ & \frac{35}{144}\,d^3\,H^6\,t^3 + \frac{685\,H^6\,t^4}{576} + \frac{25}{24}\,d\,H^6\,t^4 + \frac{115}{576}\,d^2\,H^6\,t^4 + \frac{5\,H^6\,t^5}{24} + \frac{1}{12}\,d\,H^6\,t^5 + \frac{H^6\,t^6}{72} \end{aligned}$$

In[48]:= **Expand[%47 /. {H^6 → d}]**

Out[48]=

$$\begin{aligned} & \frac{245\,519\,d}{1\,548\,288} + \frac{395\,d^2}{192} + \frac{32\,695\,d^3}{8192} + \frac{275\,d^4}{96} + \frac{62\,953\,d^5}{73\,728} + \frac{5\,d^6}{64} - \frac{5447\,d^7}{1\,548\,288} + \\ & \frac{395\,d\,t}{192} + \frac{1181\,d^2\,t}{144} + \frac{2675\,d^3\,t}{288} + \frac{1205\,d^4\,t}{288} + \frac{425\,d^5\,t}{576} + \frac{d^6\,t}{32} + \frac{1181\,d\,t^2}{288} + \\ & \frac{925\,d^2\,t^2}{96} + \frac{1315\,d^3\,t^2}{192} + \frac{175\,d^4\,t^2}{96} + \frac{85\,d^5\,t^2}{576} + \frac{925\,d\,t^3}{288} + \frac{685\,d^2\,t^3}{144} + \\ & \frac{575\,d^3\,t^3}{288} + \frac{35\,d^4\,t^3}{144} + \frac{685\,d\,t^4}{576} + \frac{25\,d^2\,t^4}{24} + \frac{115\,d^3\,t^4}{576} + \frac{5\,d\,t^5}{24} + \frac{d^2\,t^5}{12} + \frac{d\,t^6}{72} \end{aligned}$$

In[49]:= **Expand[%45 /. {t → m - (5/2) \* (d - 1)}]**

Out[49]=

$$\begin{aligned} & \frac{444\,410\,639\,d}{1\,548\,288} - \frac{66\,517\,d^2}{96} + \frac{16\,579\,621\,d^3}{24\,576} - \frac{2035\,d^4}{6} + \frac{6\,829\,033\,d^5}{73\,728} - \frac{1243\,d^6}{96} + \frac{1\,107\,385\,d^7}{1\,548\,288} + \\ & \frac{66\,517\,d\,m}{192} - \frac{49\,061\,d^2\,m}{72} + \frac{4675\,d^3\,m}{9} - \frac{27\,635\,d^4\,m}{144} + \frac{19\,745\,d^5\,m}{576} - \frac{113\,d^6\,m}{48} + \frac{49\,061\,d\,m^2}{288} - \\ & \frac{12\,595\,d^2\,m^2}{48} + \frac{28\,225\,d^3\,m^2}{192} - \frac{1705\,d^4\,m^2}{48} + \frac{1795\,d^5\,m^2}{576} + \frac{12\,595\,d\,m^3}{288} - \frac{3565\,d^2\,m^3}{72} + \\ & \frac{5225\,d^3\,m^3}{288} - \frac{155\,d^4\,m^3}{72} + \frac{3565\,d\,m^4}{576} - \frac{55\,d^2\,m^4}{12} + \frac{475\,d^3\,m^4}{576} + \frac{11\,d\,m^5}{24} - \frac{d^2\,m^5}{6} + \frac{d\,m^6}{72} \end{aligned}$$

In[50]:= **Expand[%48 /. {t → m - (5/2) \* (d - 1)}]**

Out[50]=

$$\begin{aligned} & \frac{234\,265\,319\,d}{1\,548\,288} - \frac{9885\,d^2}{32} + \frac{18\,495\,175\,d^3}{73\,728} - \frac{4975\,d^4}{48} + \frac{1\,676\,753\,d^5}{73\,728} - \frac{235\,d^6}{96} + \frac{146\,593\,d^7}{1\,548\,288} + \\ & \frac{3295\,d\,m}{16} - \frac{32\,681\,d^2\,m}{96} + \frac{61\,975\,d^3\,m}{288} - 65\,d^4\,m + \frac{2675\,d^5\,m}{288} - \frac{47\,d^6\,m}{96} + \frac{32\,681\,d\,m^2}{288} - \\ & \frac{4675\,d^2\,m^2}{32} + \frac{12\,965\,d^3\,m^2}{192} - \frac{425\,d^4\,m^2}{32} + \frac{535\,d^5\,m^2}{576} + \frac{4675\,d\,m^3}{144} - \frac{2935\,d^2\,m^3}{96} + \\ & \frac{1325\,d^3\,m^3}{144} - \frac{85\,d^4\,m^3}{96} + \frac{2935\,d\,m^4}{576} - \frac{25\,d^2\,m^4}{8} + \frac{265\,d^3\,m^4}{576} + \frac{5\,d\,m^5}{12} - \frac{d^2\,m^5}{8} + \frac{d\,m^6}{72} \end{aligned}$$

```
In[51]:= FunctionExpand[Binomial[m + 7, 7] - Binomial[7 + m - d, 7] +
  4 * Binomial[7 + m - (5 / 2) * (d - 1), 7] - 4 * Binomial[7 + m - d - (5 / 2) * (d - 1), 7] -
  3 * 5 * d * Binomial[6 + m - (5 / 2) * (d - 1), 6] + 2 * (%49) - %50]
```

Out[51]=

$$\begin{aligned}
& -\frac{234\,265\,319\,d}{1\,548\,288} + \frac{9885\,d^2}{32} - \frac{18\,495\,175\,d^3}{73\,728} + \frac{4975\,d^4}{48} - \frac{1\,676\,753\,d^5}{73\,728} + \\
& \frac{235\,d^6}{96} - \frac{146\,593\,d^7}{1\,548\,288} - \frac{1}{3072}d(-17+5d-2m)(-15+5d-2m) \\
& (-13+5d-2m)(-11+5d-2m)(-9+5d-2m)(-7+5d-2m) - \frac{1}{161\,280} \\
& (-19+5d-2m)(-17+5d-2m)(-15+5d-2m)(-13+5d-2m)(-11+5d-2m) \\
& (-9+5d-2m)(-7+5d-2m) + \frac{1}{161\,280}(-19+7d-2m)(-17+7d-2m) \\
& (-15+7d-2m)(-13+7d-2m)(-11+7d-2m)(-9+7d-2m)(-7+7d-2m) + \\
& (-7+d-m)(-6+d-m)(-5+d-m)(-4+d-m)(-3+d-m)(-2+d-m)(-1+d-m) \\
& \frac{5040}{3295\,d\,m} + \frac{32\,681\,d^2\,m}{96} - \frac{61\,975\,d^3\,m}{288} + 65\,d^4\,m - \frac{2675\,d^5\,m}{288} + \frac{47\,d^6\,m}{96} - \\
& \frac{32\,681\,d\,m^2}{288} + \frac{4675\,d^2\,m^2}{32} - \frac{12\,965\,d^3\,m^2}{192} + \frac{425\,d^4\,m^2}{32} - \frac{535\,d^5\,m^2}{576} - \frac{4675\,d\,m^3}{144} + \\
& \frac{2935\,d^2\,m^3}{96} - \frac{1325\,d^3\,m^3}{144} + \frac{85\,d^4\,m^3}{96} - \frac{2935\,d\,m^4}{576} + \frac{25\,d^2\,m^4}{8} - \frac{265\,d^3\,m^4}{576} \\
& \frac{5\,d\,m^5}{12} + \frac{d^2\,m^5}{8} - \frac{d\,m^6}{72} + \frac{(1+m)(2+m)(3+m)(4+m)(5+m)(6+m)(7+m)}{5040} + \\
& 2 \left( \frac{444\,410\,639\,d}{1\,548\,288} - \frac{66\,517\,d^2}{96} + \frac{16\,579\,621\,d^3}{24\,576} - \frac{2035\,d^4}{6} + \frac{6\,829\,033\,d^5}{73\,728} - \right. \\
& \frac{1243\,d^6}{96} + \frac{1\,107\,385\,d^7}{1\,548\,288} + \frac{66\,517\,d\,m}{192} - \frac{49\,061\,d^2\,m}{72} + \frac{4675\,d^3\,m}{9} - \frac{27\,635\,d^4\,m}{144} + \\
& \frac{19\,745\,d^5\,m}{576} - \frac{113\,d^6\,m}{48} + \frac{49\,061\,d\,m^2}{288} - \frac{12\,595\,d^2\,m^2}{48} + \frac{28\,225\,d^3\,m^2}{192} - \\
& \frac{1705\,d^4\,m^2}{48} + \frac{1795\,d^5\,m^2}{576} + \frac{12\,595\,d\,m^3}{288} - \frac{3565\,d^2\,m^3}{72} + \frac{5225\,d^3\,m^3}{288} - \\
& \left. \frac{155\,d^4\,m^3}{72} + \frac{3565\,d\,m^4}{576} - \frac{55\,d^2\,m^4}{12} + \frac{475\,d^3\,m^4}{576} + \frac{11\,d\,m^5}{24} - \frac{d^2\,m^5}{6} + \frac{d\,m^6}{72} \right)
\end{aligned}$$

In[52]:=  $s0 = \%51 /. \{m \rightarrow 0\}$ 

Out[52]=

$$\begin{aligned}
& 1 + \frac{(-7+d)(-6+d)(-5+d)(-4+d)(-3+d)(-2+d)(-1+d)}{5040} - \frac{234265319d}{1548288} + \\
& \frac{9885d^2}{32} - \frac{18495175d^3}{73728} + \frac{4975d^4}{48} - \frac{1676753d^5}{73728} + \frac{235d^6}{96} - \frac{146593d^7}{1548288} - \\
& \frac{d(-17+5d)(-15+5d)(-13+5d)(-11+5d)(-9+5d)(-7+5d)}{3072} - \\
& \frac{(-19+5d)(-17+5d)(-15+5d)(-13+5d)(-11+5d)(-9+5d)(-7+5d)}{161280} + \\
& \frac{(-19+7d)(-17+7d)(-15+7d)(-13+7d)(-11+7d)(-9+7d)(-7+7d)}{161280} + \\
& 2 \left( \frac{444410639d}{1548288} - \frac{66517d^2}{96} + \frac{16579621d^3}{24576} - \right. \\
& \left. \frac{2035d^4}{6} + \frac{6829033d^5}{73728} - \frac{1243d^6}{96} + \frac{1107385d^7}{1548288} \right)
\end{aligned}$$

In[53]:= **Factor**[%52]

Out[53]=

$$\frac{1}{1548288} (-1+d)d (-3500495 + 19507441d - 37476458d^2 + 30435862d^3 - 10691399d^4 + 1349497d^5)$$

In[54]:=  $s1 = \%51 /. \{m \rightarrow 1\}$ 

Out[54]=

$$\begin{aligned}
& 8 + \frac{(-8+d)(-7+d)(-6+d)(-5+d)(-4+d)(-3+d)(-2+d)}{5040} - \frac{787630439d}{1548288} + \\
& \frac{3317d^2}{4} - \frac{40051655d^3}{73728} + \frac{2925d^4}{16} - \frac{810011d^5}{24576} + \frac{47d^6}{16} - \frac{146593d^7}{1548288} - \\
& \frac{d(-19+5d)(-17+5d)(-15+5d)(-13+5d)(-11+5d)(-9+5d)}{3072} - \\
& \frac{(-21+5d)(-19+5d)(-17+5d)(-15+5d)(-13+5d)(-11+5d)(-9+5d)}{161280} + \\
& \frac{(-21+7d)(-19+7d)(-17+7d)(-15+7d)(-13+7d)(-11+7d)(-9+7d)}{161280} + \\
& 2 \left( \frac{1322580239d}{1548288} - \frac{162331d^2}{96} + \frac{33424421d^3}{24576} - \right. \\
& \left. \frac{2275d^4}{4} + \frac{9586153d^5}{73728} - \frac{1469d^6}{96} + \frac{1107385d^7}{1548288} \right)
\end{aligned}$$

In[55]:= **Factor**[%54]

Out[55]=

$$\frac{1}{1548288} (-1+d)d (-4964783 + 27017713d - 49890986d^2 + 37892374d^3 - 12037415d^4 + 1349497d^5)$$

In[56]:= **HK = Expand[ (%37 \* d) + 2 \* (s0 - s1) ]**

Out[56]=

$$-\frac{83 d}{48} + \frac{12\,275 d^2}{1152} - \frac{1145 d^3}{48} + \frac{13\,885 d^4}{576} - \frac{131 d^5}{12} + \frac{2003 d^6}{1152}$$

In[57]:= **Factor [%56]**

Out[57]=

$$\frac{(-1 + d) d (1992 - 10\,283 d + 17\,197 d^2 - 10\,573 d^3 + 2003 d^4)}{1152}$$

In[58]:= **K2 = Expand[ (7 d - 21) \* HK - (7 \* d - 21) ^ 2 \* (1 / 4) \* (%37 \* d) ]**

Out[58]=

$$\frac{9429 d}{512} - \frac{92\,603 d^2}{768} + \frac{1\,368\,367 d^3}{4608} - \frac{134\,785 d^4}{384} + \frac{967\,771 d^5}{4608} - \frac{46\,403 d^6}{768} + \frac{30\,457 d^7}{4608}$$

In[59]:= **Factor [%58]**

Out[59]=

$$\frac{7 (-3 + d) (-1 + d) d (4041 - 21\,070 d + 35\,720 d^2 - 22\,370 d^3 + 4351 d^4)}{4608}$$

In[60]:= **C2 = Expand[ - (1 / 24) \* (195 \* d ^ 2 - 1132 \* d + 1609) \* (%37 \* d) + (1 / 3) \* (13 \* d - 34) \* HK ]**

Out[60]=

$$\frac{240\,941 d}{27\,648} - \frac{14\,783 d^2}{256} + \frac{1\,333\,535 d^3}{9216} - \frac{22\,445 d^4}{128} + \frac{334\,055 d^5}{3072} - \frac{8423 d^6}{256} + \frac{106\,327 d^7}{27\,648}$$

In[61]:= **Factor [%60]**

Out[61]=

$$\frac{(-1 + d) d (-240\,941 + 1\,355\,623 d - 2\,644\,982 d^2 + 2\,203\,138 d^3 - 803\,357 d^4 + 106\,327 d^5)}{27\,648}$$

In[62]:= **Expand [12 \* s0 - K2 - C2]**

Out[62]=

$$-\frac{13 d}{387\,072} + \frac{19 d^3}{18\,432} - \frac{91 d^5}{18\,432} + \frac{1525 d^7}{387\,072}$$

In[63]:= **Factor [%62]**

Out[63]=

$$\frac{(-1 + d) d (1 + d) (-1 + 5 d) (1 + 5 d) (-13 + 61 d^2)}{387\,072}$$